

The UK as a Technological Follower: Higher Education Expansion, Technological Adoption, and the Labour Market

Richard Blundell, David A. Green and Wenchao Jin*

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Abstract

The proportion of UK people with university degrees tripled between 1993 and 2015. However, over the same period the time trend in the college wage premium has been extraordinarily flat. We show that these patterns cannot be explained by composition changes. Instead, we present a model in which firms choose between centralized and decentralized organizational forms and demonstrate that it can explain the main patterns. We also show the model has implications that differentiate it from both the exogenous skill-biased technological change model and the endogenous invention model, and that UK data fit with those implications. The result is a consistent picture of the transformation of the UK labour market in the last two decades.

1 Introduction

In the period extending from the early 1990s to the present, the UK economy experienced a dramatic transformation in educational attainment. Specifically, in 1993, 11% of the

*Blundell: University College London and Institute for Fiscal Studies, Gower Street, London, WC1E 6BT, UK, r.blundell@ucl.ac.uk. Green: Vancouver School of Economics, UBC, and Institute for Fiscal Studies, 6000 Iona Dr, Vancouver, BC V6T 1L4, Canada, david.green@ubc.ca. Jin: University College London, Gower Street, London, WC1E 6BT, UK, w.jin.11@ucl.ac.uk. We would like to thank the editor, referees and seminar participants at UBC and IFS for very helpful comments on earlier drafts. This research is part of the research programme of the ESRC Centre for the Microeconomic Analysis of Public Policy at IFS. We are grateful to the ESRC, grant number RES-000-23-1524, for financial support. The usual disclaimer applies.

population held a university degree. This percentage doubled by 2006 and tripled by 2016. In this paper we examine the impact of that increase on the UK labour market, using our findings as a basis for contributing to the ongoing discussion about the interaction of educational attainment and technological change.

There is a strong consensus among economists that the Information Technology (IT) revolution has played a central role in determining wage and employment outcomes in many economies in the last four decades and that the effects of education should be viewed in conjunction with that revolution (see [Acemoglu and Autor \(2011\)](#) for a comprehensive review of the literature on these topics, which started with [Katz and Murphy \(1992\)](#)). Most famously, changes in the wage distribution have been described as a race between skill-biased demand shifts emanating from IT innovations and increases in skills generated by changes in education levels ([Goldin and Katz, 2008](#)). The core idea underlying this consensus is that the new technologies are complementary with skills. Intertwined with the broad literature on the effects of technology on the wage structure in general is a literature on skills, IT, and the organizational structure of the firm (e.g., [Bresnahan et al. \(2002\)](#); [Caroli and Van Reenen \(2001\)](#); [Bloom et al. \(2014\)](#), which build on [Becker and Murphy \(1992\)](#) and [Radner \(1993\)](#) among others). This literature seeks to look inside the ‘black box’ of the firm to understand how skills complement IT. Its main message is that IT, by altering information flows and communications within firms, implies a shift in the optimal organization of the firm toward a form that is more decentralized and flexible. Decisions, information transfer, and co-ordination of tasks happen throughout the organization instead of through top-down direction as in the previous, Taylorist form - the form in which tasks are broken into small sub-components with central direction. The shift in organizational form is the channel through which more educated workers benefit from the broad technological change since human capital investment gives workers greater ability to deal with increased change and decision making and makes them relatively more productive in the new environment. On the other side, a large literature on polarization argues that IT replaces routine tasks to the detriment of less educated workers ([Acemoglu and Autor \(2011\)](#)). Our approach, both theoretically and empirically, incorporates both the decentralization and routinization elements of the IT revolution and how they intersect with educational change.

Much of the empirical work and the clear majority of the theorizing on the interaction between education and technological change has been done on the US economy. However, there are good reasons to believe that the US is the technological leader in this period and, because of that, may exhibit special relationships between technological change

and education that do not apply even to other advanced economies. Given this, we view the UK educational expansion as an opportunity to study the relationship between education and technological change in a technological follower, as we believe the UK has been in terms of skill biased technologies and firm organizational forms. We will argue that taking this perspective has an impact on which model of technological change and education one adopts. In particular, we argue for a model in which firms choose among existing technologies rather than one with new invention. Our claim is that a technological choice model provides a natural explanation for a remarkable fact for the UK: that its very substantial increase in education level was accompanied by a complete lack of change in the university-high school wage differential. We present a model that captures this fact but also has further testable implications that we show are supported in the data.

Our key message is that technological change is not one size fits all. Many papers look for evidence of the importance of technological change in common movements in the relation between educational attainment and wage differentials across countries. The argument being that if new technologies are accessible in all developed countries then, conditional on mediation through relative skill supply shifts, it should act as a common force showing up in the same way in all developed countries. In contrast, differential movements in the combination of educational attainment and skill based wage differentials across countries is taken as evidence of the impact of other, non-technological factors (e.g., [Caroli and Van Reenen \(2001\)](#)'s examination of French and English data or [Antonczyk et al. \(2010\)](#)'s assessment of education and wage movements in the Germany and the US). In contrast, we argue that the same changes in factor supplies interacting with the same technology can dictate quite different wage outcomes for two countries depending on whether they are leaders or followers in the adoption of that technology.

The paper proceeds in six sections including the introduction. In the second section, we establish the core patterns for the UK, relying largely on Labour Force Survey (LFS) data between 1993 and 2016. We show that, despite a rapid increase in the proportion of university graduates, the college wage premium is flat across our time period.¹ We demonstrate the robustness of the two findings: they cannot be explained as, for example, declines in the actual wage differential that are masked by changes in composition. We consider compositional changes related to increases in the female participation rate, the shift toward more advanced university degrees over time, the difference between the

¹Note that the period investigated in the paper is after the period when the college wage premium in the UK increased substantially ([Machin and McNally, 2007](#)).

public sector and the private sector, and the substantial increase in immigration. We also consider changes in unobserved abilities, using a bounding approach. None of these exercises alters the core result that the education wage differential was essentially unchanged during a period of rapid educational growth.

The combination of an increase in the supply of education and no change in the educational differential points to an offsetting relative demand shift favouring more educated workers. Such a shift has, of course, been the focus of considerable investigation, with a common conclusion that technological change associated with the IT revolution has been a key driving force. In the third section, we investigate competing models of technological change: the canonical model of exogenous skill biased technological change; models in which increases in education induce skill biased invention; and models of technological choice, in which firms choose among existing technologies. To test among the models, we employ wage and relative wage regressions derived from a general production function that nests all three possibilities. Based on estimates of those regressions, we argue that a model with exogenous technological change (either in its classic form or in a task based form) cannot explain the skill and wage patterns in the UK data. In particular, in the context of those models our estimates would imply that skilled and unskilled labour are nearly perfect substitutes and that there has been no exogenous skill biased demand shift, neither of which seems reasonable. This echoes previous papers that conclude that the canonical model also does not fit more recent US data ([Beaudry and Green \(2005\)](#); [Card and DiNardo \(2002\)](#); [Acemoglu and Autor \(2011\)](#)). The implied substitution patterns are also relevant for empirical specifications derived from the endogenous invention model when holding technological change constant. For those specifications, as well, the findings of near perfect substitutability and no ongoing skill bias to demand shifts do not match the model. Implications from the endogenous invention model when not holding technological change constant also do not fit with the UK data patterns.

We also present evidence that, viewed through the lens of an endogenous invention model, the US is a strong candidate for being the technological leader where the new skill biased inventions were made. It had both a higher level of education and a higher amount of investment in IT before any other developed economies. The UK, on the other hand was a laggard in educational attainment. We argue that once the UK did start to increase the educational level of its workforce, its firms could choose to pick up the technologies and organizational forms already developed in the US. In that sense, it is more natural to think of the UK in the context of the third type of model: a model of endogenous technological choice.

In the fourth section, we set out a model of endogenous technological choice which has the ability to capture the core data patterns and the results of our estimation. The model is a variant of models in [Rosen \(1978\)](#) and [Borghans and ter Weel \(2006\)](#) which focuses on the role of decentralization of decisions and information. It is also related to the model of endogenous technological choice in [Beaudry and Green \(2003\)](#). Firms use skilled and unskilled labour and choose between an older, centralized mode of operation and a newer, decentralized mode. The model endogenously generates an unchanging college wage premium. This was the point of using this type of model, and so that outcome provides no proof of the model’s relevance. However, the model also generates testable added implications about the pattern of employment in manager positions for skilled and unskilled workers as the relative supply of skilled workers increases as well as strong implications about the form of the aggregate production function.

We examine these empirical implications of our model in section five. In that section, we also investigate further implications by examining the relationship between the educational composition of the workforce and the extent to which workers feel they control how they do their own work using matched worker-workplace survey data from the UK Workplace and Employer (WERS) data. We show that the areas where the increases in the BA proportion were largest had the greatest uptake of decentralized organizational forms. We establish that this is a causal relationship using an IV strategy using a combination of parental education and the population share of the birth cohorts most affected by the educational increase, measured in 1995 (i.e., before the entry of the most affected cohorts into the labour force). We view this as a credible strategy since the validity of the instrument just requires that differences in fertility rates across areas were not driven by changes in firm organizational forms twenty years later. Thus, the data fits with a model in which increased educational attainment induces more and more firms to choose a decentralized organizational form. One interesting implication of the model that is confirmed in this data is that increases in education levels in an area induce larger increases in individual decision making among less educated than among more educated workers. This arises because under the old, centralized technology, more educated workers were disproportionately managers and were already making their own decisions. It is for the less educated that decentralization is a particularly big revolution.

In section five, we also briefly provide evidence that several other developed and developing economies in this period also experienced a combination of a rapid increase in educational attainment with little change in the education wage differential. That is, in our terms, the UK was not the only technological follower. The sixth section of the

paper contains conclusions.

We are not the first researchers to note the substantial increase in degree-holding in the UK. For example, [Carpentier \(2004\)](#) documented the trend in student numbers from 1920 to 2002, showing that it increased sharply around the early 90s. He also showed a reduction in university expenditure per student around the same time. Many other studies have also documented the substantial increase in the share of graduates in the 1990s or across cohorts [OLeary and Sloane \(2005\)](#); [Walker and Zhu \(2008\)](#); [Green and Zhu \(2010\)](#); [Devereux and Fan \(2011\)](#).

Previous papers have also noted the lack of a reduction in the college wage premium over time or across recent UK cohorts ([Machin and McNally \(2007\)](#); [McIntosh \(2006\)](#); [Walker and Zhu \(2008\)](#)). However, those papers either appeal to offsetting relative demand shifts stemming from exogenous skill biased technical change or do not attempt to explain the lack of change in the relative wages at all. We add to the previous literature, in part, by providing an explanation that does not rely on exogenous skill biased demand shifts that just happen to be the right size to match the change in educational attainment across a range of years. Instead, we present a model in which this pattern arises endogenously, which has ramifications for how we think about the interactions of technological change, factor supplies, and factor demand. We also differ from earlier studies in our explicit emphasis on the firm organization part of the process - that is where our empirical work focuses. Combined, these give us new insights into how technological change affects economies. Overall, we view studying the UK as an opportunity to examine the impact of education policy on technological adoption and, through it, on wages in the situation that is likely relevant for most countries - being a technological follower.

2 Data and Core Patterns

2.1 Data

Our main empirical work is based on the demographic, education, employment, wage, and occupation variables in the UK Labour Force Survey (LFS). The LFS is a representative quarterly survey of approximately 100,000 adults that is the basis for UK labour force statistics. It is similar in nature to the US Current Population Survey (CPS) which we use as a comparison. We make use of UK LFS data running from the first quarter of 1993 to the last quarter of 2016.

Consistent definitions of education levels over time are obviously important in our

investigations. The LFS asks respondents about their highest level of educational qualification, with the potential categories changing over time. We take advantage of detail in the potential responses to construct six more aggregate categories that are consistent over time. For our main discussion, we then further aggregate those categories into three broader groups: a university degree level or above; secondary or some tertiary education below a university degree level; and below secondary qualifications. We draw the bottom line of secondary education as Grade C in the General Certificate of Secondary Education (GCSE), which are exams that students take at age 16 after 11 years of formal schooling. The GCSEs mark the first major point of exit from education in England: around one fifth of the working-age population have GCSEs Grade C or above or equivalents as their highest level of qualification in 2016. We consider a grade of at least C to be equivalent to High School graduation (HS) in the US because the proportion of people strictly below the threshold in the UK is close to the proportion of HS drop-outs in the US.² Under UNESCO’s International Standard Classification of Education (ISCED 2011), both US High School Diploma and UK’s GCSE Grade C or above fall into ISCED level 3 “upper secondary education”. We have investigated alternative definitions of education groups and they make little difference to our main results.³ We restrict our samples to people between ages 20 to 59 because the education qualification question was not asked of people over age 60 before 2007 unless they were working at the time of the survey.

Wages are surveyed in the first and fifth quarters an individual is in the survey. We use the hourly wage derived from the weekly wage in the main job and actual weekly hours. Our sample contains 30,000-75,000 wage observations per year. As we are interested in the real cost of labour to firms, we deflate wages by the GDP deflator⁴.

In places, we use the U.S. CPS to form a comparison. We again use individuals aged 20 to 59. The data is from the Outgoing Rotation Group samples. Following Lemieux (2006), we do not use observations with imputed wages when calculating wage statistics. Wages and employment status refer to the week prior to the survey week, and we only use wage and occupation data for individuals who are employed in the

²For example, 10.6% of 25-34 year olds in the US are HS drop-outs in 2012. Coincidentally, the proportion of this age group in the UK who do not have qualifications equivalent to or higher than GCSE grade C is also 10.6% ; and 19.8% have qualifications equivalent to GCSE grade C and no higher qualifications.

³These are reported in Appendix B.4. One particular alternative we have tried is to define the UK HS group by A-levels instead of GCSEs. A-levels are typically taken at age 18 and are required for university admission.

⁴Source: we use the variable ‘GDP: Total implicit price deflator’ in the dataset called ‘MEI Original Release Data and Revisions’ from OECD.stats.

reference week. We aggregate the U.S. workers into three education groups: high school drop-outs; high school graduates (which includes workers with some or completed post-secondary education below a Bachelor’s degree); and university degree holders (Bachelors and higher).

2.2 UK Wage and Educational Attainment Movements

2.2.1 Changes in educational attainment

We begin with a figure showing the level of university attainment over time for the UK, with the US as a benchmark. We will use the shorthand of calling the group with university degrees BA’s, even though it includes other types of Bachelors degrees and more advanced degrees. For both the US and the UK, we summarize the data by plotting year effects from an exercise in which we first calculate the BA proportion for the set of cells defined by year and 5-year wide age ranges then regress those proportions on a complete set of year and age range dummies. We control for age in this way because we are concerned that the movement of the baby boom through the age structure will affect our BA proportion measure.

Figure 1 contains plots of the year effects for the BA proportion for both the UK and the US. The figure includes year effects from the General Household Survey (GHS) for the UK for the years before 1993 along with the same proportions from the LFS starting in 1984.⁵ The sample sizes for the GHS are small, especially for the more educated, so we don’t use it in our main analysis, but it does provide longer term context for the LFS data patterns. For the overlapping years, both of the UK datasets show a gradually increasing trend, although the level differs. As shown in Figure 1, the BA proportion in the UK showed a gradual increase in the 1970’s and 1980’s but it was still only about 0.13 in 1990, half of the value for the US in that year. Beginning around 1993, however, the UK proportion underwent a rapid acceleration. By 2010, it had surpassed the US.⁶

The big increase in the UK proportion in the BA group starting in the mid-1990s corresponds to a rapid increase in higher education enrolment from 1988 to 1994. This increase has been documented in many studies (O’Leary and Sloane (2005); Carpentier (2006); Walker and Zhu (2008); Green and Zhu (2010); Devereux and Fan (2011)) and has been used as an arguably exogenous source of variation in studies of the causal

⁵The LFS underwent significant changes in 1984 and in 1992. Before 1984, it was a bi-annual survey. From 1984 to 1991 it was annual. From 1992Q2 onwards, it was quarterly.

⁶The rate of increase and the catch-up to the US is even clearer when the data is plotted by birth cohort (Appendix A).

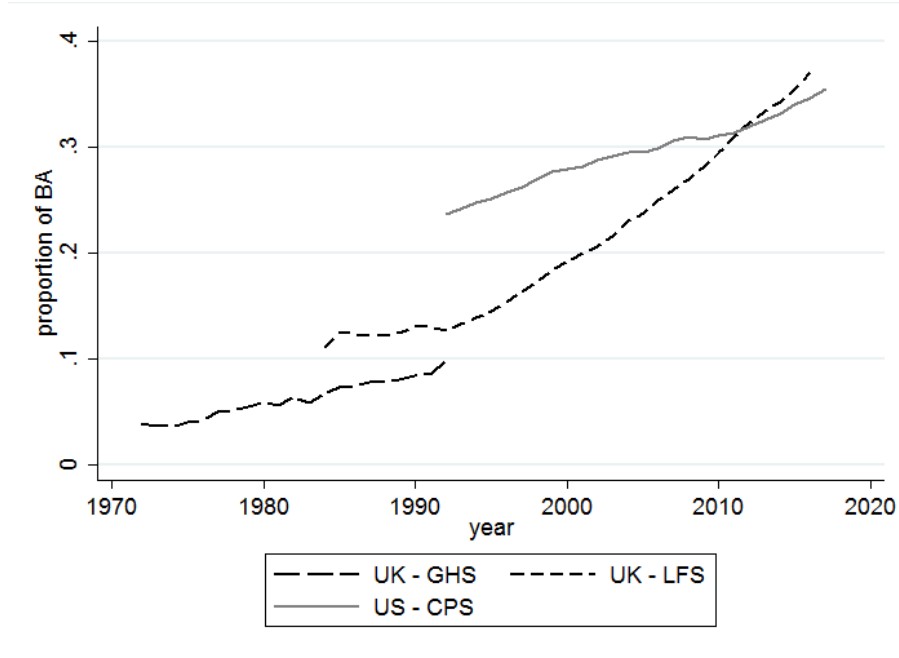


Figure 1: Proportion BA for the UK and US

Notes: BA refers to individuals who have a bachelors or higher degree. We aggregate each dataset to the level of year and 5-year age band, and regress the BA proportion on year dummies and age-band dummies. The proportion BA numbers are year effects from these regressions plus the level in 1992 for the 30-34 age band.

Source: Authors' calculation from the UK Labour Force Survey, the UK General Household Survey, and the US Current Population Survey.

impact of education [Devereux and Fan \(2011\)](#). The expansion of higher education over these decades reflects a sequence of specific policy choices made by the UK government. Further details are provided in the appendix [B.4](#).

2.2.2 Changes in relative wages

The second main pattern relates to wages. In [Figure 2](#) we plot the ratio of BA to high school median hourly wage by year for the UK. We will refer to this ratio as the college wage premium. As with the BA proportion, the plot corresponds to year effects from a regression in which age is held constant.⁷ The striking point in this figure is its flatness. Over the span of years from 1993 to 2016, the wage ratio shows only minor fluctuations

⁷In [Appendix B](#), we present the college wage premium over the life-cycle by birth cohort. The differential is increasing over age in a concave pattern for each cohort. Because of this life-cycle pattern, one would expect the education wage ratio for the economy as a whole to increase as the population in our 20-59 sample ages, due to the baby boomers getting older. Holding age constant allows us to look past these composition related changes to the underlying wage changes.

around a flat line. The absence of significant changes to the relative wages is consistent with previous studies which found the UK graduate wage premium to be stable in the 90s and early 2000s [Chevalier et al. \(2004\)](#); [McIntosh \(2006\)](#); [Machin and Vignoles \(2006\)](#); [Machin and McNally \(2007\)](#); [Walker and Zhu \(2008\)](#).⁸ The flatness of the ratio seems to us to be striking in light of the near tripling of the proportion of the working age population with a BA over this same period. Our goal in this paper is to provide an explanation for this pair of patterns.

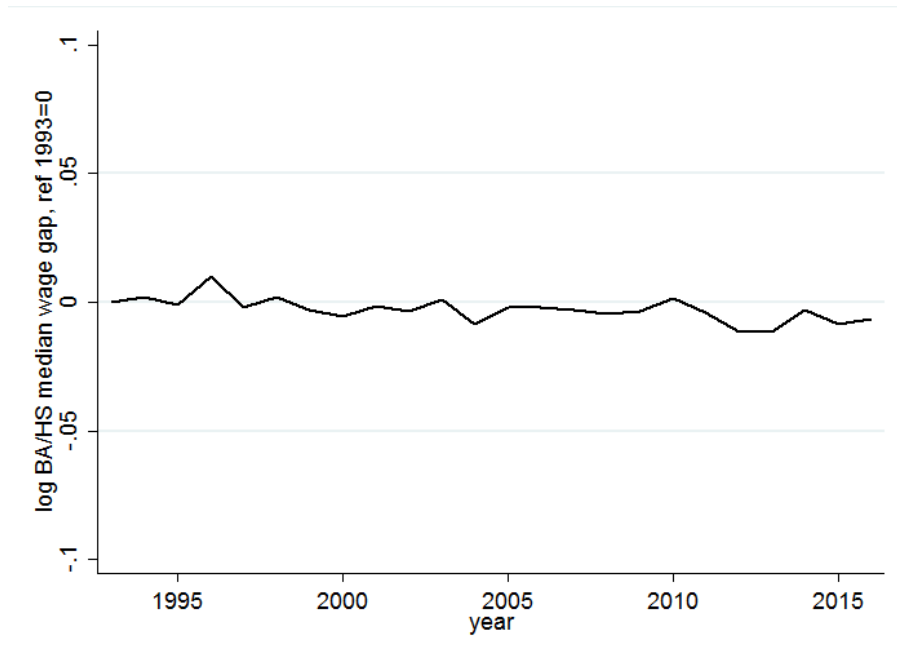


Figure 2: Ratio of BA median wage to that of high-school graduates 1993-2016, UK

Notes: Wage is hourly. The sample is 20-59 year olds in LFS 1993-2016. BA refers to individuals who have a bachelors or higher degree. We aggregate LFS to the level of year and 5-year age groups, and regress the log BA to HS median wage ratio on year dummies and age-band dummies. The figure plots the estimated year effects normalized to zero in 1993.

2.3 The Effects of Composition Shifts on the Core Patterns

One possible explanation for why such substantial increases in educational attainment were associated with little or no change in educational wage differentials is that com-

⁸Two earlier papers [OLeary and Sloane \(2005\)](#); [Walker and Zhu \(2005\)](#), using data up to 2003, found the university premium to have fallen somewhat over the cohorts that experienced the higher education expansion. However, the authors later revised their cohort conclusions with more years of LFS data in [Walker and Zhu \(2008\)](#).

positional shifts are obscuring the true patterns. To see this, it is helpful to think of workers as bundles of efficiency units of tasks. More able workers supply a larger number of efficiency units per hour worked, and, in a standard neoclassical model, their observed wages will reflect this. As a result, observed average wages can increase either because of increases in the market price per efficiency unit or because the composition of workers shifts in the direction of a higher average number of efficiency units per worker. Since our result is that the observed college wage premium has not fallen as we might expect, the scenario of greatest potential interest is one in which the price differential for BA versus HS tasks declines while the differential in average efficiency units between BA and HS workers increases.

2.3.1 Observable Characteristic Composition

Perhaps the most obvious compositional shift in terms of observable worker characteristics is related to the increase in female labour force participation. If the added female entrants with BA's are successively more able (compared to the added HS females) then their entry could hide a decline in the education differential in prices per efficiency unit. However, even the most cursory glance at the data indicates that gender composition shifts are not a source of problems since the wage patterns are the same for males and females. In Figure 3 we plot the Proportion of BA's and the college wage premium for males and females separately (again, obtaining year effects from regressions including age polynomials). For both genders, we see the dramatic increase in the BA proportion after 1993, with a faster increase for females. The wage differential remains flat over time for each gender, with each series showing nearly identical values for the differential in 1993 and 2016, and so a change in weighting between men and women would not alter the overall wage picture.

In Appendix B.6, we present several further exercises. First, we consider the increase in the proportion of university degree holders with post-graduate degrees. We show that replotting the wage line in figure 2 including and not including workers with post-graduate degrees among the BA's does not change the main pattern: both lines show nearly identical values in 1993 and 2016. This is a reflection of the fact that, while the proportion of workers with a postgraduate degree increased rapidly, the proportion of university graduates with these degrees was still small at the end of our period. Second, we consider immigration as another potential source of compositional change since the proportion of UK workers born outside the UK doubled over the past two decades and immigrant returns to education are lower than those of the native born (Dustmann et al. (2013)). However, the combination of strong increases in education with no accompanying changes

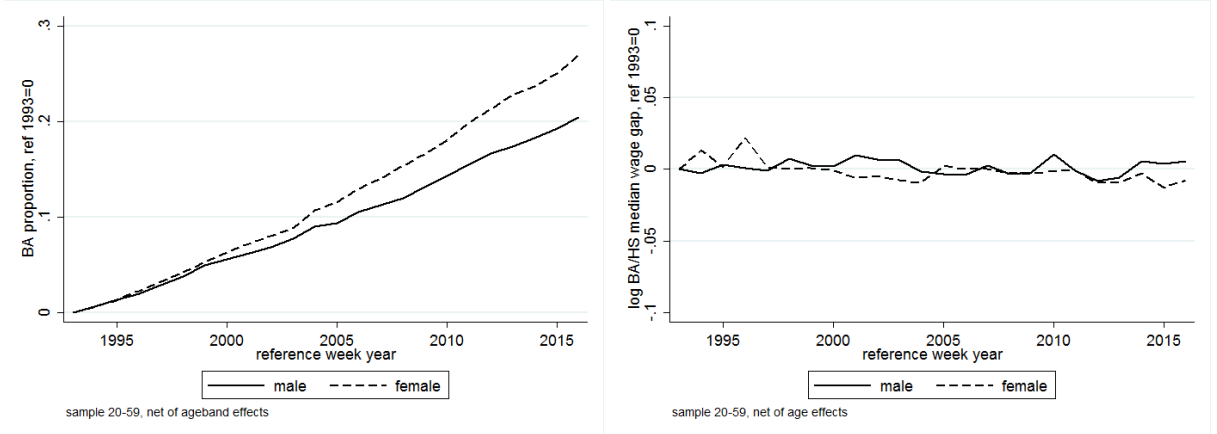


Figure 3: UK year effects on BA proportion and college wage premium by gender

Note: The year effects use the same sample selection and regression specification as for Figure 2 but here are separated by gender.

in the college wage premium is present even if we look at the UK nationals alone, implying that composition changes related to immigration are not driving our main patterns. We also break the data down into public versus private sector employment and wages. Over the sample period, the public sector's employment share has remained around 25%. Both sectors saw very large increases in the BA proportion, with somewhat faster increases in the private sector. Both sectors again experienced relatively flat movements in the college wage premium, though the private sector trend is slightly more negative (amounting to about a 3% decline over the period from 1994 to 2016 as shown in Figure 13).

Overall, we conclude that shifts in composition with respect to observable worker characteristics cannot explain our main pattern of substantial education increases paired with an invariant education wage premium.

2.3.2 Unobservable Characteristic Composition

It is still possible, of course, that changes in the composition of unobservable characteristics has shifted across education groups in a way that could explain the wage patterns. As higher education expands, it draws in pupils from a wider and wider range of prior attainment and perhaps innate ability. The expansion of university education in the UK after 1988 came with a fall in per student resources and was accomplished in part by transforming polytechnic institutions into universities. Both of those changes might also have had a negative impact on the quality of courses and hence of graduates. Thus, it seems possible that the average quality of BA workers has declined across cohorts. It

is important to note, however, that this does not necessarily imply that the observed college wage premium is biased one way or the other relative to the composition constant differential. The quality of HS-educated workers is also likely to fall if the more able individuals among those who would have stopped at a HS education level in earlier cohorts now go to university and if some of those who would have been HS dropouts previously now obtain secondary qualifications. Thus, it is theoretically ambiguous whether the ability-composition constant college wage premium is greater or smaller than the observed one.

The idea that BAs have a lower and wider range of quality after the higher education expansion has been advocated in [OLeary and Sloane \(2005\)](#) and [Walker and Zhu \(2008\)](#). Both papers use quantile regressions to estimate the university wage premium across different periods or cohorts, and they report a greater decline in the premium at lower quantiles than at higher quantiles. While it's tempting to interpret such results as evidence of declining quality of BAs at the lower end of the BA wage distribution, examining the wage distributions for BA and HS workers separately suggests a different conclusion. Working with 5-year wide birth cohorts, in [Appendix B.5](#) we show that the decline in the wage differential at lower quantiles is driven by relative increases in lower end wages for the HS-educated. The 50-10 differential of the BA wage distribution is unchanged across cohorts entering the labour market in our period. Thus, it is difficult to conclude that the fall of the graduate premium at lower quantiles is due to a greater deterioration in the quality of BAs than HS workers at their respective lower ends.

In [Appendix B.7](#), we also present a bounding exercise to examine the limits of the potential impact of shifts in the distribution of unobservable characteristics on the college wage premium. We work at the level of 5-year birth cohorts because any such shifts would be clearest in looking at different cohorts of potential university graduates. Our exercise follows [Manski \(1994\)](#), [Blundell et al. \(2007\)](#) and [Lee \(2009\)](#), and works directly from a bounding approach in a Roy Model context set out in [Gottschalk et al. \(2014\)](#).

Underlying our approach is an hierarchical model of ability. In this model, there is a single, unidimensional ability that is more productive the higher is an individual's education level. Under standard assumptions on costs, higher ability individuals sort to higher levels of education. In this situation, there is a set of individuals (or, more properly, ability levels) who choose to go to university even in the pre-expansion period when universities were more costly to access. With the expansion of the university system these "university stayers" continue to get a higher education but they are joined by a set of "university joiners" who have been induced to enter university by the declining

costs. Thus, the pre-expansion wage distribution for BA's consists only of university stayer wages while the post-expansion BA distribution includes both stayers and joiners. We have no way of identifying who is a stayer and who is a joiner in the post-expansion distribution, but by making extreme assumptions on which workers are joiners, we can construct extreme bounds on the median wages for stayers. Comparing those bounded values to the median wage for BA's before the expansion (who, remember, consist only of university stayers), we get bounds on movements in the median university stayer wage. Since the stayers are a consistent group over time, these bounds reflect wage movements for a composition constant group.

We can make one of two extreme assumptions in order to form bounds. In the first, the 'joiners' are the lowest wage earners in the post-expansion cohort wage distribution. Thus, the 'stayers' wage distribution can be obtained by trimming from the lower tail of the observed wage distribution the proportion by which the set of university educated workers has expanded between the two cohorts (where the proportion is expressed as a proportion of the post-expansion set of BA workers). At the other extreme, the 'joiners' would be better workers. But as [Gottschalk et al. \(2014\)](#) show, under a standard Roy model, the 'joiners' can be at best as good as the 'stayers'. If they were better then they would already have entered the BA sector. Thus, the other bound is the actual observed post-expansion distribution. Performing an analogous exercise with HS workers, we can form bounds on movements in the high school wage and on the college premium.⁹

We present detailed results from the bounding exercise in the Appendix. The nature of the exercise is such that the bounds are defined as movements relative to a base cohort - in our implementation, the 1965-69 cohort. That cohort entered university age just before the major policy generated university expansion that began in 1988 and had a university graduate proportion of 0.16. The following two 5-year birth cohorts (born 1970-74 and 1975-79) represent the main part of the increase in educational attainment. For the 1975-79 cohort, the proportion graduating university reached 0.34. The bounds on the change in the college wage premium between the 1965-69 and 1975-79 cohorts range between an upper bound of 0 and a lower bound of -0.05. That is, even under extreme assumptions, the movements in the relative wage distribution and the proportion

⁹In forming the ratio, we use the benchmark case where the upper bound scenarios for the BA and HS workers correspond to one another (i.e., the movements out of the top of the HS distribution become the movements into the bottom of the BA distribution). We can then obtain one bound on the movement in the university - high school wage differential by taking the difference between the upper bound on the movement in the university median and the upper bound on the movement in the high school median. The other bound is the actual change in the median wage ratios.

of each cohort who graduated university fit with very small changes in the college wage premium. In the following cohorts - ones over which the proportion with a university degree increased at a much slower rate - the bounds move to around -0.15 for the 1985-89 cohort. Re-examining Figure 2 in light of this finding, it is possible to see a small (though statistically insignificant) decline in the college premium after 2010. To the extent this is true, it would suggest a decline in the premium that occurs after the main increases in the educational supply. We will return to that possibility later in our discussion. But, our overall conclusion from the bounding exercise is that, under this model of ability, selection on unobservables cannot explain why we do not see a large decline in the education wage differential for the cohorts with the largest increase in their education level.

3 Technological Leadership and Models of Technological Change

To this point we have established that since the mid-1990s, the UK experienced a substantial upgrading in the education level of its workforce but virtually no change in the wage differential between university and high school educated workers. The obvious implication is that the increase in the relative supply of more educated workers was exactly offset by an increase in the relative demand for more educated workers. That type of skill biased demand shift is, of course, the focus of a very large literature in which much of the attention focuses on the role of technological change. We are convinced by papers such as [Bresnahan et al. \(2002\)](#), [Caroli and Van Reenen \(2001\)](#), and [Bloom et al. \(2014\)](#) which argue that the key technological change in recent decades is broader than just the use of computer hardware and software in specific tasks, taking in changes in organizational form that make use of newly invented IT features. For that reason, we will couch our investigations of the impact of technological change in that wider, organizational context.

One can think of the interaction of increased human capital attainment with technological change in terms of three main models. The first is one in which the technological change is exogenous: a new technology is introduced for an unspecified reason and is so dominant in terms of cost savings over existing technologies that it is adopted on a wide scale. Wage differentials are then determined by the interaction of relative demand shifts arising from this technological change (hinging on the skill bias of the technological change) and shifts in supply. Early versions of this model that focused directly on the college wage premium have generally been shown not to fit the data well ([Beaudry and](#)

Green (2005); Card and DiNardo (2002); Acemoglu and Autor (2011)) but the more recent literature on polarizing changes in technology also has this broad form (e.g., Autor and Dorn (2013)). In all of these models, wage differentials reflect the classic race between technological change and education, with wages in higher skilled groups (defined by education or occupation) rising less if educational policy generates increases in the supplied labour in that group ((Goldin and Katz, 2008)).

The second model type is one in which the invention of new technologies is a function of movements in the relative factor endowments in an economy. Thus, an increase in the education level in an economy provides an incentive for inventors to create new technologies that are relatively intensive in the use of higher educated labour (Acemoglu (1998), Kiley (1999)). In this case, the relative increase in demand for skills is actually induced by the increase in their supply. Acemoglu (2007) shows that in cases where innovation is created by government funded research or by monopolistic or oligopolistic firms, if the elasticity of substitution between skilled and unskilled labour is high enough then an increase in the relative supply of skilled workers can induce an increase in the relative wage of the skilled workers. In this sense, in the context of this model, attempts to combat inequality by increasing educational attainment could backfire.

The third type of model is one in which a set of technological options already exist and firms choose among them. These endogenous choice models have the structure of a 2 sector by n factor trade model, where the sectors correspond to different technologies, and inherit implications of that model. In particular, if $n > 2$ and all factors are inelastically supplied then these models can yield the same implications as the induced invention models, i.e., that increases in the relative supply of skill can generate increases in the skilled wage differential (Beaudry and Green (2003); Beaudry et al. (2010)). On the other hand if all but two of the factors are perfectly elastically supplied (as one might expect if new organizational capital, for example, requires a one time investment but widely accessible information thereafter) then even large increases in the relative supply of educated labour will leave skill group wages unchanged if the economy remains within a region in which both the new and old technologies are in use (the cone of diversification) (Beaudry and Green (2003)).¹⁰ We believe this class of models fits with the spirit of the literature on decentralization and organizational form which, starting with Milgrom and Roberts (1990)'s seminal contribution, often approaches organizational form as something

¹⁰Note that this is different from the first, competitive model in Acemoglu (2007). In that model, firms choose among technologies but those technologies are included as another input in a standard, unitary production function. The technological choice models we are referring to involve choosing among completely different technologies with different substitution elasticities.

firms optimally choose given existing options (e.g., [Bresnahan et al. \(2002\)](#); [Caroli and Van Reenen \(2001\)](#)). It also follows a line of reasoning dating back to [Griliches \(1958\)](#) which emphasize endogenous adoption of technologies as the cost of adoption changes (see, for example, [Doms et al. \(1997\)](#) and [Borghans and ter Weel \(2007\)](#)).

Deciding which of these models is relevant for an economy is important because, as we have just described, they can have quite different implications for the effect of education policy on inequality. But which model is relevant is potentially context contingent. There may be technologies that are so superior that the exogenous technical change model is clearly relevant (though we suspect those situations are extremely rare). On the other hand, in economies that are technological leaders in time periods when new technological possibilities are opening up, the induced invention model may be more appropriate. However, for other, following economies (and even in the technological leaders in periods after the initial invention is complete) the endogenous technological choice models, with firms choosing from an already invented set of options, may be the most relevant.

Much of the theorizing about these different models has been done with the US economy and US stylized facts in mind. But the US context may be quite unique. In particular, we will argue that there are good reasons to believe that the US has been a technological leader in the development of skill biased technologies and their associated organizational forms in recent decades. The UK - and, potentially, other developed economies - are, then, technological followers. In the remainder of the paper, we investigate the claim that the UK is a technological follower and that, as a result, endogenous technological choice models best describe the functioning of its economy.

3.1 Testing Among Models of Technological Change

In this section, we use an empirical specification derived from a relatively general production function with UK data to establish the claim that the exogenous technological change and endogenous innovation models do not match patterns in the UK data market in recent decades. Given that, in subsequent sections, we set out a model of endogenous technological choice and investigate its implications, including for the wage specifications derived and implemented in this section.

To investigate the various models, we derive an empirical specification that nests all three models. Here, we provide a brief description of the derivation, with details in [Appendix A](#). We adopt a specification set out in [Beaudry and Green \(2005\)](#) in which there is an aggregate production function given by, $F(\theta_{st}S_t, \theta_{ut}U_t, K_t)$, where S_t is skilled

labour used in production, U_t is unskilled labour, K_t is capital, and θ_{st} and θ_{ut} are skilled and unskilled labour enhancing technological change parameters, respectively. Given the focus of the existing literature and to keep the discussion simple, we assume that technological change is labour enhancing, implying that our specification does not nest factor neutral technical change. We discuss the implications of using a form of factor neutral technical change in Appendix B.1. We will also assume that $F(.,.,.)$ is constant returns to scale. Apart from that, the production function is left purposefully general so that it can be seen as reflecting any of the three models of technological change. Because we are concerned that there could be age effects arising from the movement of different sized cohorts into the education system, we follow Card and Lemieux(2001) in assuming that both skilled and unskilled labour can be written as CES aggregates of labour supplied by workers of different ages, i.e., $S_t = (\sum_j \Gamma_j S_{jt}^{\frac{\sigma_a-1}{\sigma_a}})^{\frac{\sigma_a}{\sigma_a-1}}$ and $U_t = (\sum_j \Omega_j U_{jt}^{\frac{\sigma_a-1}{\sigma_a}})^{\frac{\sigma_a}{\sigma_a-1}}$, where S_{jt} is the amount of skilled labour from age group j that is employed in period t , U_{jt} is defined analogously, Γ_j and Ω_j are age specific factor augmenting parameters, and σ_a is the elasticity of substitution between age groups within a skill group. In our estimation, we use over time variation within geographic sub-regions in the UK but in our initial exposition we will focus on a single region, suppressing the regional subscript.

Assuming competitive labour markets and employing a log linear approximation, we obtain,

$$\ln w_{ujt} \approx \ln \Omega_j - \frac{1}{\sigma_a} \ln \tilde{U}_{jt} + \ln \theta_{ut} + \alpha_1 \ln\left(\frac{S_t}{U_t}\right) + \alpha_1 \ln\left(\frac{\theta_{st}}{\theta_{ut}}\right) + \alpha_2 \ln\left(\frac{K_t}{\theta_{ut} U_t}\right) \quad (1)$$

and,

$$\ln w_{sjt} \approx \ln \Gamma_j - \frac{1}{\sigma_a} \ln \tilde{S}_{jt} + \ln \theta_{st} + \beta_1 \ln\left(\frac{\theta_{st} S_t}{\theta_{ut} U_t}\right) + \beta_2 \ln\left(\frac{K_t}{\theta_{st} S_t}\right) \quad (2)$$

where, $\ln \tilde{S}_{jt} = (\ln S_{jt} - \ln S_t)$ and $\ln \tilde{U}_{jt}$ is defined analogously. Concavity of the production function implies $\beta_1 - \beta_2 \leq 0$ and $\alpha_1 + \alpha_2 \geq 0$.

The difference between the two log wage expressions gives

$$\begin{aligned} \ln \frac{w_{sjt}}{w_{ujt}} \approx & (\ln \Gamma_j - \ln \Omega_j) - \frac{1}{\sigma_a} (\ln \tilde{S}_{jt} - \ln \tilde{U}_{jt}) + (\alpha_2 - \beta_2) \ln \theta_{ut} + (\beta_1 - \beta_2 - \alpha_1) \ln\left(\frac{S_t}{U_t}\right) \\ & + (1 + \beta_1 - \beta_2 - \alpha_1) \ln\left(\frac{\theta_{st}}{\theta_{ut}}\right) + (\beta_2 - \alpha_2) \ln\left(\frac{K_t}{U_t}\right) \end{aligned} \quad (3)$$

Equation (3) is a generalization of the specification in Card and Lemieux(2001). In that paper, as in most papers in the skill biased technical change literature, only a relative wage equation is estimated. But there is relevant information in the underlying wage

equations as well, and we will focus on the skilled wage equation along with the wage ratio equation. With estimates of those two, the unskilled wage equation is redundant.

In order to take the skilled wage equation and the relative wage equation to the data we need to address the fact that the productivity parameter ratio ($\ln(\frac{\theta_{st}}{\theta_{ut}})$) and the θ_{ut} parameter that enter both equations are unobserved. We address these issues using the approach in [Beaudry and Green \(2005\)](#), capturing general productivity increases with measured TFP and allowing for exogenous skill-biased shifts using a quadratic function of time. This allows for a bit more flexibility than the common linear skill biased technical change assumption, which is obviously nested in this specification.

Based on this, we arrive at an estimable specification for the skilled wage equation similar to the one in [Beaudry and Green \(2005\)](#), given by:

$$\ln w_{sgjt} = b_{0j} + b_{0g} + b_0 t + b_1 t^2 + b_2 \ln\left(\frac{S_{gt}}{U_{gt}}\right) + b_3 \frac{\ln TFP_t}{(s_t^u + s_t^s)} + b_4 \ln\left(\frac{K_t}{U_{gt}}\right) + b_5 \ln \tilde{S}_{gjt} + \epsilon_{1gjt} \quad (4)$$

where ϵ_{1gjt} is an error that contains approximation error and is assumed to be independent of the right hand side variables. We also obtain a relative wage specification given by:

$$\ln \frac{w_{sgjt}}{w_{ugjt}} = d_{0j} + d_{0g} + d_0 t + d_1 t^2 + d_2 \ln\left(\frac{S_{gt}}{U_{gt}}\right) + d_3 \frac{\ln TFP_t}{(s_t^u + s_t^s)} + d_4 \ln\left(\frac{K_t}{U_{gt}}\right) + d_5 (\ln \tilde{S}_{gjt} - \ln \tilde{U}_{gjt}) + \epsilon_{2gjt} \quad (5)$$

where, again, ϵ_{2gjt} corresponds to approximation error. Note that both equations include a complete set of age band effects. In addition, we have introduced a subscript, g, corresponding to geographic region. We include a complete set of region effects (d_{0g}) and, so, are using within-region and age group, over-time variation. We construct the wage and employment variables at the region by age group by time level, but it is important to highlight that neither the TFP_t variable components nor K_t have g subscripts, i.e., the relevant values for both are assumed to be at the national level. For TFP_t , this reflects an assumption that technologies are available equally in all regions of the country. The same assumption underlies the lack of a g subscript on the time trend coefficients. For K_t , the corresponding assumption is that the capital market is national. With capital and technology defined at the national level, we use regional level data to see how regional variation in skill supplies alter sub-national differences in technological adoption and, so, wages. We view differences in regional outcomes within a common capital market as a good scenario in which to examine implications of the relationship between

skill supplies and wages. The detailed derivation of these equations in the Appendix provides the direct mapping of the b and d coefficients onto the underlying structural (α, β , and σ_a) parameters. We also include there a discussion of the conditions under which our specification reduces to the [Card and Lemieux \(2001\)](#) version of the canonical specification, which does not include capital or TFP terms.

The exogenous technical change model and the induced innovation model have similar testable implications for the estimated coefficients in our model. In particular, in the canonical exogenous technical change model, the d_2 coefficient equals $-\frac{1}{\sigma}$, where σ is the elasticity of substitution between skilled and unskilled labour, and must be negative ([Card and Lemieux \(2001\)](#)). Further, the coefficients on the time variables in the wage ratio equation should imply a positive and significant trend, representing the exogenous technological shift favouring skilled workers. Given our expanded specification, skill biased technical change could, alternatively, show up as a positive and significant coefficient on $\frac{\ln TFP_t}{(s_t^u + s_t^s)}$ in the wage ratio equation, implying that observed technological change favours skilled workers. In the endogenous innovation model, holding technology constant (as we do using the combination of the time trend and TFP), d_2 is also equal to $-\frac{1}{\sigma}$ and, so, faces the same restrictions as with the exogenous technological change model ([Acemoglu, 2007](#)), equation (18)). Further, if we estimate a specification in which we do not control for technology then the coefficient on $\ln(\frac{S_{gt}}{U_{gt}})$ in the wage ratio equation is an amalgam of the substitution effect and a potentially offsetting innovation effect that would raise the relative wage of skilled workers. The theory implies a connection between the estimated coefficients with and without controls for technology: if the elasticity of substitution estimated when controlling for technology is large then the effect of a shift in relative skill supply on the relative wage should be large and positive. Thus, in order to test the implications of the innovation model, we implement our full specification as well as a specification in which we do not include either time or TFP variables. For comparison to previous estimates, we also estimate the [Card and Lemieux \(2001\)](#) variant of the canonical model for the wage ratio, i.e., a specification that includes all the variables in (5) except $\ln TFP_t$ and $\ln(\frac{K_t}{U_t})$. In the appendix, we present further specifications in which we drop $\ln(\frac{K_t}{U_t})$ and replace it with the log price of capital, $\ln r_t$. Our conclusions are robust to these variations.

We use UK LFS data from 1993 to 2016, restricting our sample to 20-59 year olds for whom we observe wages and education. We aggregate to the level of cells defined by 5-year wide age groups and geographic regions, which allows us to control for compositional changes associated with the growing importance of London and other urban centres in

our time period. For sample size reasons, we pool the data in 3 year groups.¹¹

Within each age x region cell, we obtain the median real log wage for BA and for HS workers. We take the difference of those to form our wage gap dependent variable. We measure S_{gjt} and U_{gjt} as the total number of hours worked by BA and HS workers, respectively, who are in region g , age-band j and year t . We measure S_{gt} and U_{gt} as the simple sums of S_{gjt} and U_{gjt} across age groups within a region.¹² We scale S_{gjt} , U_{gjt} , S_{gt} and U_{gt} so that the aggregate hours supplied each year $\sum_g (S_{gt} + U_{gt})$ matches the national time series from the Office of National Statistics (ONS).¹³ We obtain aggregate TFP series, capital and aggregate hours from the ONS.¹⁴

It is worth emphasizing that our estimates are based on variation within region x age cells over time. In figure 4, we show the variation we are using by plotting long differences (between 1993-1995 and 2014-2016) in $\ln \frac{w_{sgjt}}{w_{ugjt}}$ against long differences in $\ln \frac{S_{gjt}}{U_{gjt}}$ for all our regions for one of our age groups (30 to 34 year olds). Plots for other age groups show the same pattern. In particular, there is considerable variation in changes in $\ln \frac{S_{gjt}}{U_{gjt}}$ across regions, ranging from just over 1.1 log point increase over the 20 years in Northern Ireland to a high of over 1.5 log points in London and with an even spread in between. Matching that is little change in the within region/age group wage ratio, with most of the long term changes in the ratio being under 10% in absolute value. The correlation between the two series is only 0.15 and is not statistically significantly different from zero. When we put $\ln \frac{S_{gt}}{U_{gt}}$ instead of $\ln \frac{S_{gjt}}{U_{gjt}}$ on the x-axis, we get a similar pattern of weak correlations comparing only between regions. Thus, our data has considerable over-time variation in changes in employment ratios across regions matched with small changes and

¹¹The three year groups are 1993-95, 1996-98, etc.. We use the LFS "Regions of Usual Residence" as our definition of geographic regions. There are 19 such regions including, for example, London, Rest of South East, Greater Manchester, and the Western Midlands. These regions are consistently defined over the whole of our sample period. Sample size issues related to the reporting of wages prevents us from using a more detailed geography such as the one used in the organizational forms exercise later in the paper. We treat our production function as being at the level of the region, implying that all of our variables now have a g , for geographic region, subscript. The only exceptions are the capital and TFP variables. We assume that both capital and technological ideas flow freely across the regions in the country, implying that the country-aggregate levels of those variables are relevant.

¹²This deviates from the theory in which the aggregates are functions of $\sigma_a, \Gamma_j, \Omega_j$. We do this for simplicity and transparency so that we aren't forcing this element of our specification on the data. Since our estimates of σ_a imply very high substitutability across age groups, the results change very little when using the CES aggregates with estimated parameters rather than simple sums.

¹³The simple sum of hours in our sample every year would deviate from the true aggregate hours because education is missing to varying degrees over time and our sample selects 20-59 year olds only.

¹⁴The TFP series is the annual series of multi-factor productivity from ONS' release "Multi-factor productivity estimates: Experimental estimates to Q2 2017". Our capital measure is the annual series called "Contribution of capital services to GVA growth (percentage points)" in the same ONS release. Aggregate hours is "labour hours" from the same ONS release. This ONS release can be found [here](#).

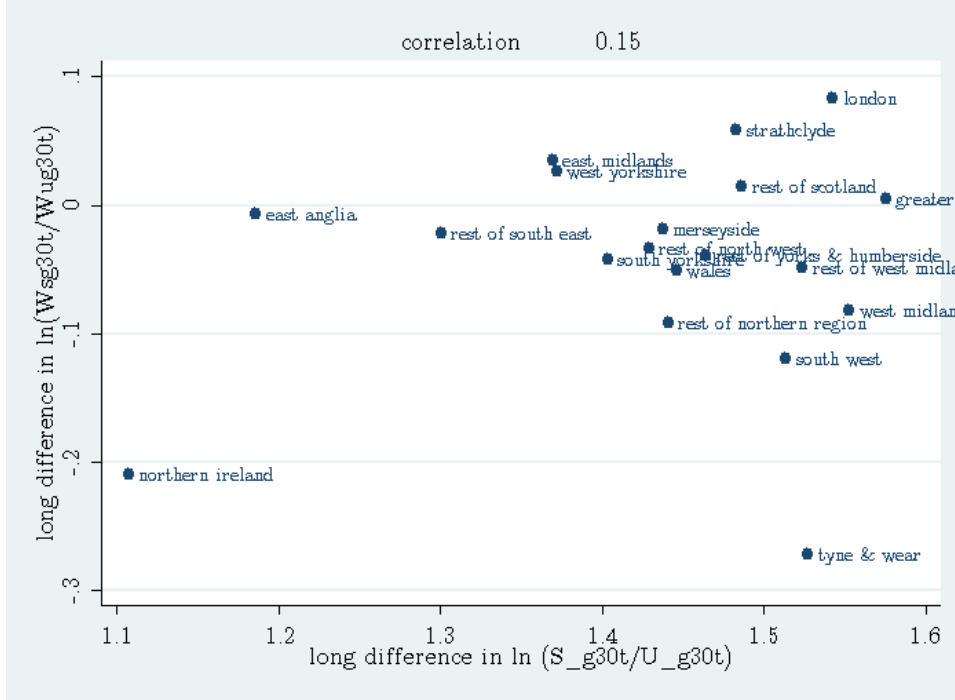


Figure 4: Changes in Employment and Wage Ratios by Region, 1995 - 2016

Note: The variables are the difference between 1993-1995 and 2014-2016 in the log ratio of employment (x-axis) and median wages (y-axis) of BA to HS workers for each region. The data is for 30 to 34 year olds in each year.

little variation in the change in the wage ratio. This core moment in the data is what is driving our estimate of the coefficient on $\log S_{gt}/U_{gt}$ in Table 1.

We present the results from our specifications in Table 1. The first two columns contain estimates of the skilled wage equation and the wage ratio equation by OLS. The second two columns contain 2SLS estimates aimed at addressing the potential endogeneity of the employment levels of the inputs. We instrument for $\ln \frac{S_{gt}}{U_{gt}}$ by using the education reform. In particular, we form a Bartik style instrument in which we interact the proportion of the population in a region in 1993 (the start of our data) who were born in 5 year-wide birth cohorts with the growth in the proportion of that cohort who obtained a BA at the national level. The idea behind this instrument is that regions with a higher proportion in the cohorts that were most directly affected by the education reforms (those born between 1970 and 1974 and between 1975 and 1979) would face a stronger increase in the relative supply of skilled labour for reasons that have to do with historical fertility patterns that are plausibly independent of later education trends. We also construct an instrument as the interaction of the proportion of the parental genera-

tion for the 1970-1979 birth cohorts who themselves had a BA with the national growth rate in the proportion of workers with a BA. This is intended to capture the idea that children in locations with more educated parents were more likely to take advantage of the education reforms. Both instruments are strong predictors of $\ln \frac{S_{gt}}{U_{gt}}$ in the first stage and do not suffer from weak instrument issues by any standard test. Using similar logic to the second instrument, for each birth cohort in each region, we construct the proportion of the ‘parental’ cohort (the one born 25 years earlier) with a BA. We interact that proportion with the growth rate in the proportion with a BA for the specific child’s cohort at the national level. Here too, the idea is that the growth in the BA share for an age group in a region will be related to the education level of the parents for that age group combined with the general increase in education level for their cohort. We use this as an instrument for $\ln \frac{S_{gjt}}{U_{gjt}}$ but have to restrict our attention to age 20 to 44 year olds because the first stage is weak when we include older individuals since there is little variation in the proportion of the parents’ generations with a BA for the older age groups. Finally, we instrument for $\ln \frac{K_t}{U_t}$ using the interest rate.

The theory underlying our specifications implies several restrictions. The results reported in Table 1 have not imposed these restrictions; imposing them would make little difference to the key estimates and we will show them in Appendix A.

3.2 Assessing the Exogenous and Endogenous Skill Biased Technological Change Models

The estimates from our wage specifications do not fit with either the canonical exogenous SBTC model or the induced skill biased innovation model. The first strike against these models is the lack of any substantial effects of the skill supplies on the wage ratio. The estimated coefficients on $\log S_t/U_t$ in column (1) (OLS) and column (3) (IV) of Table 1 are statistically insignificant and have the wrong sign according to the theory. Results from alternative specifications presented in Appendix A all show this same pattern. Moreover, the lower bound of the confidence interval for the IV estimate in Table 1 (-0.05) is very small compared to the earlier use literature (e.g., -0.7 in [Katz and Murphy \(1992\)](#)). Thus, even in a generous interpretation, the coefficient would imply very high and possibly perfect substitutability between skilled and unskilled labour. This is very problematic for both the exogenous and induced innovation models since changes in relative demand created by either exogenous or endogenous technical change cannot move relative wages if the skill groups are perfect substitutes. As a side point, the age-specific skill supply

coefficient is also close to zero (-0.038 in the OLS, and the wrong sign in the IV), implying a huge substitution elasticity between age groups (above 25). By comparison, [Card and Lemieux \(2001\)](#) estimated this elasticity to be in the [4,6] range.

Table 1: Skilled Wage and Wage Ratio Regressions: UK, 1993-2016

	$\ln \frac{w_{sgjt}}{w_{ugjt}}$	$\ln w_{sgjt}$	$\ln \frac{w_{sgjt}}{w_{ugjt}}$	$\ln w_{sgjt}$	$\ln \frac{w_{sgjt}}{w_{ugjt}}$	$\ln \frac{w_{sgjt}}{w_{ugjt}}$
t	0.006 (0.008)	0.021** (0.007)	-0.025* (0.012)	0.000 (0.012)		-0.00330 (0.005)
t^2	-0.000 (0.000)	-0.001*** (0.000)	0.000 (0.000)	-0.000 (0.000)		
$\ln S_{gt}/U_{gt}$	0.047 (0.087)	-0.034 (0.081)	0.256 (0.156)	-0.168 (0.163)	0.002 (0.010)	0.056 (0.084)
$\ln \frac{TFP_t}{\text{laborshare}_t}$	-0.004 (0.121)	0.315** (0.113)	0.091 (0.104)	0.474*** (0.109)		
$\ln K_t/U_t$	-0.104* (0.049)	-0.073 (0.046)	0.212 (0.167)	0.488** (0.177)		
$\ln \tilde{S}_{gjt}/\tilde{U}_{gjt}$	-0.038 (0.023)		0.015 (0.038)		-0.036 (0.023)	-0.036 (0.023)
$\ln \tilde{S}_{gjt}$		-0.025 (0.021)		-0.133 (0.156)		
IV	no	no	yes	yes	yes	no
N	1208	1208	760	760	760	1208

Notes: standard errors are shown in parentheses. The regression is at the level of 19 regions, 5-year-age-bands and 3-year-periods. The sample without IVs consists of 20-59 year olds. Whenever we use IVs, the sample is restricted to 20-44 year olds. The first 2 columns are the OLS estimation of the two equations. SURE results would be very similar and not shown here. The next 2 columns contain 2SLS estimates. 3SLS estimates would also be very similar to the 2SLS ones. The fifth column does not control time trend or TFP and the sixth is comparable to [Card and Lemieux \(2001\)](#). All specifications include complete sets of age-band and region dummies. *** p<0.01, ** p<0.05, * p<0.1

The second strike against the exogenous SBTC model is found in the coefficients on the time and time squared variables in the wage ratio equations. Recall that these are intended to capture the path of the ongoing skill biased technological changes. The IV estimates imply a negative trend while the OLS estimates imply technological change effects that are small and move from positive in early years to negative in later years. These results are robust to different specifications. Such a pattern, in which technical change is small and either against skilled labour from the outset (IV) or turning against it in later years (OLS) does not fit with the exogenous technical change model.

These conclusions are reinforced in the last column of the table which contains esti-

mates from the implementation of the the classic [Card and Lemieux \(2001\)](#) specification that includes only the linear time trend, the overall skill supply ratio, the skill supply ratio at the age group level, and a complete set of age and region effects. From this specification, we can see that our estimates of the skill supply and time effects in our main specification are not being determined by the inclusion of the TFP and capital variables. The estimated coefficients on both the time trend and the relative supply variables are statistically insignificant and of the wrong sign. The coefficient on the age group specific relative supplies is also small and statistically insignificant. At best, using the extremes of the confidence intervals, these estimates imply that skilled and unskilled labour are close to perfect substitutes, different age groups are close to perfect substitutes, and there is little or no ongoing skill biased technical change. We view these data patterns as a repudiation of the exogenous skill biased technical change model for the UK in the period after 1992.¹⁵

The estimated TFP effects provide further evidence against both the exogenous and endogenous skill biased technological change models. The TFP variable has a small and statistically insignificant effect on the wage ratio in column 3 of the table. Combined with the positive and statistically significant effect of TFP on the skilled wage in the estimates in column 4, the implication is that there is technological growth in this period but that skilled and unskilled workers benefit from it to an equal degree. Thus, the data does not fit with technology, as captured by TFP, being skill biased: the core feature of both of the first two technological change models.¹⁶

All of these implications apply to both the exogenous and endogenous skill biased technological change models, but the endogenous technological change model has added implications. In particular, if we do not control for technological change then the impact of changes in the skill ratio on the wage ratio no longer has a determinate sign. The negative substitution effect that is estimated when controlling for technological change is combined with an effect on innovation that can generate offsetting, skill biased demand shifts. Under some circumstances, the latter effect dominates and the estimated coefficient in the relative wage regression without technology controls can be positive. In column 5, we present estimates of the wage ratio equation without the TFP and trend

¹⁵These patterns are robust to imposing the theoretical restrictions on coefficients in equations (4) and (16) and to excluding London, out of concerns that it is big enough to be driving the results on its own.

¹⁶A referee pointed out that problems with the exogenous and endogenous SBTC models can also be demonstrated in a calibration exercise. In Appendix B.3, we show that if one assumes typical values from the US literature for σ and σ_a then the combination of the implied path for $\ln \frac{\theta_{st}}{\theta_{ut}}$ of observed TFP implies a very strongly declining path for θ_{ut} that is unrealistic.

variables. We also drop $\ln \frac{K_t}{U_t}$ in order to obtain a specification similar to what is implied in [Acemoglu \(2007\)](#). The estimated coefficient on the relative skill supply variable is close to zero and statistically insignificant. For this to be the case, σ , the elasticity of substitution between skilled and unskilled labour should be near 2 in the endogenous innovation models in ([Acemoglu, 2007](#)) and ([Acemoglu and Zilibotti, 2001](#)). Instead, our estimates in columns 1 and 3 have the opposite sign and even the lower bound of the estimates indicate much larger σ values. The lower bounds of estimates in columns 1 and 3 would imply the effect of the relative skill supply in column 5 should be much larger. Either way, the data patterns are not consistent with the implications of the endogenous innovation model.

One possible response to our concerns about the model of exogenous SBTC of the type embodied in [Card and Lemieux \(2001\)](#) is that it is an older version of these models which has been supplanted by models of technological change and polarization. This has happened, in part, because other papers have similarly concluded that the exogenous skill biased technical change model does not fit even the US data well either (e.g.,([Card and DiNardo \(2002\)](#); [Beaudry and Green \(2005\)](#); [Acemoglu and Autor \(2011\)](#))). To look further into the role of polarization in the UK wage and employment structure, in [Table 2](#) for 30-34 year olds, we present average real wages (in the first column of the first panel) and proportions of employees (in the first column of the second panel) in each of 9 one digit occupations in 1993. The occupations are ranked by their average real wage. In the second columns in each panel we present the change in either wages or proportions between 1993 and 2016.

The second column for employment proportions shows an approximate U-shaped pattern, with growth in employment shares in the top three occupations, declines in the middle (largely routine) occupations and growth in personal services. The relationship is not perfect since the lowest-paid occupation (“elementary”) shows a decline, but the pattern is broadly one of polarization. However, when we hold the education composition constant between the cohorts (in the last column), there are small declines in employment in the top three occupation groups and essentially no change in processing and skilled trades in the middle. There is some added evidence of relative growth at the bottom of the distribution. The main conclusion, however, is that the right branch of the U-shape in employment growth in the UK is entirely attributable to the education shifts. That is, occupation shifts appear to us to be of secondary importance relative to education shifts in determining the changes in the wage structure in the UK. Given that, we do not believe that polarization/task based versions of the exogenous SBTC theory provide a

Table 2: Changes between 1993 and 2016, by occupations, at age 30-34

occupation	mean real wage		employment shares		
	w_{1993}	%change observed	$share_{1993}$	change observed	change reweighted
Professional occupations	15.00	0.184	0.111	0.070	-0.016
Associate professional and technical	14.00	0.149	0.159	0.029	-0.022
Managers and senior officials	13.06	0.257	0.151	0.010	-0.020
Skilled trades	10.19	0.128	0.133	-0.034	0.013
Administrative and secretarial	9.85	0.227	0.134	-0.046	-0.047
Process, plant and machine operatives	9.10	0.097	0.090	-0.038	-0.005
Personal service	7.89	0.194	0.055	0.032	0.052
Sales and customer service	7.63	0.229	0.060	0.002	0.018
Elementary occupations	7.09	0.184	0.107	-0.026	0.028

Notes: Real wage is in 2012 prices, deflated by GDP deflator. The final column reweights the employment shares of occupations using the education split in 1993 of 30-34 year olds.

useful lens through which to understand the specific wage and employment patterns we are examining.

Taken together, we view the patterns of changes in wage levels, wage ratios, skill ratios, TFP, and capital for the UK in the last two decades as firmly rejecting both the exogenous skill biased technological change model and the endogenous skill biased innovation model for the UK for this period. Our view is that the endogenous innovation model is better suited to explaining movements in economies that are technological leaders where the innovation is taking place and that this does not describe the UK in this period. We elaborate on this claim in the next section.

3.2.1 Induced Technological Change and Technological Leadership

Induced technological innovation models focus on the expansion of the technological frontier. As such, they are about countries which are the technological leaders and would seem to provide a better explanation for movements in leader than follower economies. Working within the induced innovation model, the country that is most likely to be the leader in skill biased technological innovation will be the one with the highest share of skilled workers. A high share provides an incentive for innovator firms to invent machines or forms of organization that complement skills. In 1980, on the cusp of the computer revolution, the US was the leading developed economy in terms of education level. In that year, 22% of the US population aged 25 to 64 had a tertiary education, which was

by far the highest in the OECD ([Lee and Lee \(2016\)](#)).¹⁷ Thus, incentives for innovators to generate human capital intensive technologies would have been highest in the US. Moreover, the US has had the highest ratio of investment in ICT (Information, Computers, and Technology) capital to total non-residential gross fixed capital throughout the 1985 to 2010 period (OECD(2017)). The idea that the US is the innovation leader is also supported by evidence in [Bloom et al. \(2012\)](#) showing that US multinationals use a more decentralized structure relative to both domestic firms and multinationals from other countries even when all are observed operating in the same economy (the UK).

On the other side, there is also good reason to believe that the UK is a follower in the area of skill biased technologies and their associated organizational forms.¹⁸ Certainly, the UK was well behind the US in educational attainment at the beginning of the computer revolution. This can perhaps be most clearly seen in data organized by birth cohort. For the cohort born between 1955 and 1959 in the UK (and who would have turned 25 in the early 1980s, at the outset of the computer revolution), 12% held a university degree by age 30 compared to 24% for the same cohort in the US.¹⁹ For the cohort born a decade later, the numbers were 16% for the UK and 27% for the US - the UK was still a laggard. Thus, viewed through the lens of the theory of induced invention, we would not expect the UK to have been a leader in skill-biased innovation. However, because of the educational reforms described earlier, by the cohort born between 1975 and 1979 (who turned 25 in the early 2000s), the UK had surpassed the US with 34% attaining a university degree in the UK compared to 32% in the US. That increase in the educational attainment of new labour market entrants in the UK could have provided the conditions for firms to adopt the technologies previously developed in the US. Interestingly, the proportion of investment that was in ICT capital shot up in this decade in the UK, approximately doubling at the same time the proportion of new labour market entrants with a university education also doubled (OECD(2017)).²⁰ Further, the evidence in [Bloom et al. \(2012\)](#) about use of

¹⁷The next highest were Canada at 18% and Australia and New Zealand at about 15%, with the remainder of the OECD decidedly lower.

¹⁸Classifying the UK as a technological follower could imply that we can analyse its wage patterns as the equivalent of a Southern economy in the analysis in [Acemoglu and Zilibotti \(2001\)](#). In their discussion, Northern economies innovate in response to relative skill changes in their workforces as described earlier. Southern countries, in contrast, do not innovate and take the technological level invented in the North as given. However, with no innovation response channel in the South, increases in the relative supply of skill in their workforces will necessarily induce a decline in the skilled-unskilled wage ratio. As we have seen, this does not fit with the wage patterns in the UK in recent decades.

¹⁹These figures are computed from the UK LFS for the years 1992 to 2015 and the Outgoing Rotation Group sample from the US Current Population Survey for the same years.

²⁰The proportion of total non-residential fixed capital investment in ICT increased by 88% in the UK between 1990 and 2000. Only Finland and South Korea had faster growth in this proportion in this

decentralized organizational forms also suggests that UK firms were following rather than leading. They argue that UK firms were laggards in adopting decentralized structures because of regulation based inflexibilities. We offer an alternative explanation: that at the time of the development of the new IT related structures, the lower education level in the UK implied it was less profitable for UK firms to adopt the new approach. Then, as the UK education level increased, the UK underwent a technological transformation. We think that these patterns fit most naturally with models of technological choice and we turn to a model of this form in the next section.

4 A Model of Educational Changes, Technological Change and Decentralization

In this section, we set out a model of technological choice in a situation where newly invented technologies involve decentralized organizational forms made possible by IT innovations. We derive implications of the model at the macro level that we compare to our production function estimates and at the micro level that we investigate with workplace data in the following sections.

The general framework we consider is one in which firms can choose to produce a single output either with a centralized (C) technology or a decentralized (D) technology. Having a single output is intended to emphasize the nature of these technologies as general purpose technologies that could be applied to the production of any product. Following [Rosen \(1978\)](#) and [Borghans and ter Weel \(2006\)](#), we will characterize production in engineering terms as having a Leontieff form in which a continuum of tasks, x , defined on the unit interval are required to produce an output.²¹ The amount of each task required to produce one unit of output is given by the continuous function, $\alpha(x)$, $x \in [0,1]$. The tasks are performed by two types of workers: U (unskilled) and S (skilled). Total hours of work are inelastically supplied by each type of worker. Workers of each type are described by capacity functions, $\tau_l(x)$, which are continuous functions defined on $[0,1]$ determining the amount of time a worker of type $l = U, S$ needs to produce the amount of task x required for one unit of output. Further, we assume that tasks are

decade. In comparison, the proportion grew by 37% in the US.

²¹This general form for production has become somewhat common in models of technological change, tasks, and polarization. For example, a variant of it is used in [Acemoglu and Zilibotti \(2001\)](#), and [Acemoglu and Autor \(2011\)](#) use this approach to provide a framework for interpreting existing research on tasks and technological change. Our model differs in the way we introduce decentralization and in our assumption that firms can choose between two such technologies.

ordered from least to most complex and that S workers have comparative advantage in more complex tasks, i.e., $\frac{\tau_S(x)}{\tau_U(x)}$ is decreasing in x .

Rosen (1978) shows that based on such a specification, one can derive a production function defined over n_s and n_u (the number of hours of S and U labour used, respectively) in which the firm allocates a given amount of S and U to each task in order to maximize output. In particular, firms will allocate skill groups according to their comparative advantage in the sense that there will be a task ρ such that all tasks, $0 \leq x \leq \rho$ are assigned to U workers and, conversely, all tasks $\rho < x \leq 1$ are assigned to S workers. Further, ρ is declining in $\frac{n_s}{n_u}$. Thus, if the relative number of S workers is small then they will only be assigned to the most complex tasks and as that relative number grows, they will be moved progressively further down the list of tasks ranked by complexity. The marginal rate of technical substitution between S and U equals $\frac{\tau_S(\rho(n_u, n_s))}{\tau_U(\rho(n_u, n_s))}$, where we have written ρ as a function of n_u and n_s . Thus, profit maximizing firms will hire numbers of hours of U and S labour to equate the marginal rate of technical substitution to the wage ratio, $\frac{w_S}{w_U}$ (where, w_S and w_U are the skilled and unskilled hourly wages), allocating those hours optimally according to comparative advantage over the tasks required to produce. The result is a production function that reflects the efficiencies from taking account of the comparative advantage of the two types of workers and which is, itself, not necessarily Leontieff in form. In this sense, the ultimate production function reflects more than just the engineering ‘recipes’ since it includes the optimal allocation of workers across the task combinations specified in the recipes.

As Rosen (1978) demonstrates, and as we draw in figure 1, in the case with two types of workers (our case), the unit output isoquant intercepts both axes. The intercept on the N_u (number of unskilled workers) axis equals $\int_0^1 \tau_U(x) dx$. As we move away from that intercept to the left, we begin to introduce S workers, replacing the U workers in the most complex tasks. Thus, the slope of the isoquant is given by $\frac{\tau_S(\rho(n_u, n_s))}{\tau_U(\rho(n_u, n_s))}$ and comparative advantage dictates the standard convex shape. The N_s intercept is given by $\int_0^1 \tau_S(x) dx$.

We will consider an economy with two possible ‘recipes’ or technological forms. The first is centralized and takes the form as set out above, where we will now write the technological requirements function as $\alpha^C(x)$ and the amount of time a worker needs to complete the number of tasks needed for a unit of output as, $\tau_l^C(x)$. In order to match patterns in the data, we delineate management tasks from other tasks. In the centralized technology, management tasks are necessary in order to co-ordinate the other tasks and the producers of the other tasks just focus on production of their part of the process,

leaving communication and co-ordination to the managers. We will arbitrarily denote tasks on the interval $[\theta, 1]$ as management tasks. To keep the exposition simple, we will assume that the α and τ functions are continuous from above and below at θ .

The alternative technological form is decentralized. [Caroli and Van Reenen \(2001\)](#) describe modern organizational forms as being ‘delayed’ with ‘some decision-making being transferred downstream.’ Multi-tasking is also an important feature of this organizational form with the benefits that the firm becomes more flexible and managers have to spend less time monitoring and co-ordinating workers ([Bloom et al. \(2014\)](#)). Thus, rather than having workers performing physical tasks without regard to others and having a manager who co-ordinates the outcome, in a decentralized form, workers both produce and co-ordinate with other task producers. As a result, less of the pure management task is needed. All of this is made possible by (i.e., is complementary with) IT technological change, which reduced the cost of diffuse information transfer.

We capture the differences in the decentralized form relative to the centralized form, first, by assuming that there is a lower requirement for the pure management tasks in the new form:

$$\alpha^D(x) = \lambda \alpha^C(x), \forall x \geq \theta \quad (6)$$

where, the D superscript denotes the decentralized technology, and $\lambda < 1$. For simplicity, we will assume that the requirements for the other tasks remain the same, i.e., $\alpha^D(x) = \alpha^C(x), \forall x < \theta$.

Following much of the literature on technical change and the labour market, we also assume that skilled workers are better at working with the new organizational form ([Caroli and Van Reenen \(2001\)](#); [Bresnahan et al. \(2002\)](#)). We represent this by assuming that skilled workers are perfect multi-taskers and can perform each of the non-management tasks in the same amount of time as before, performing the new, associated communications while they are doing them without extra effort (thanks to IT). For unskilled workers, performing each non-managerial task now requires more time since working with the new IT is more difficult for them. Further, skilled workers are able to take advantage of the new technology in management tasks while unskilled workers are not. Thus,

$$\tau_S^D(x) = \tau_S^C(x), \forall x < \theta \quad (7)$$

and

$$\tau_U^D(x) = \gamma \tau_U^C(x), \forall x < \theta \quad (8)$$

with $\tau_U^D(x) = \tau_U^C(x), \forall x \geq \theta$, $\tau_S^D(x) = \lambda \tau_S^C(x), \forall x \geq \theta$ and $\gamma > 1$. We view this specification as capturing the notion of decentralization in papers such as [Lindbeck and Snower \(1996\)](#); [Caroli and Van Reenen \(2001\)](#); [Bresnahan et al. \(2002\)](#), and [Bloom et al. \(2012\)](#): that it is an organizational form in which decision making and communications are spread throughout the firm rather than being done by a small cadre of managers. We could allow for decentralization forms in which communication and decision making are differentially allocated across tasks but elect for the simpler form in which they are essentially allocated evenly across the non-manager tasks for expository clarity.

The literature emphasizes that decentralization has been enabled by the advent of IT. Much of the recent work on IT and the labour market also emphasizes impacts of the new technology in replacing routine tasks that tend to lie in the middle of the wage distribution. Following [Borghans and ter Weel \(2006\)](#) and [Acemoglu and Autor \(2011\)](#), we can model this effect by having the α values in middle tasks substantially reduced under the new (D) technology. Essentially, the idea is that IT capital performs those tasks and, thus, less labour is required in them. As described in [Acemoglu and Autor \(2011\)](#), the result will be a polarization in employment, with relatively more employment in low and high complexity jobs compared to those in the middle. However, this will not alter our main points about movements in educational wage differentials set out below. For that reason, we will not explicitly include the reductions in middle α 's in our analysis for simplicity.

Given this setup, if there were only U workers in the economy then all firms would use the C technology since it would be cheaper at any given unskilled wage. Conversely, if there were only S workers in the economy, firms would use only the D technology. But we will start by assuming that the endowment of S and U workers in the economy is such that both technologies are in use (returning to the conditions under which that is true momentarily). We also assume that these are general purpose technologies that can be used for producing any good. Thus, to simplify, we assume both are used to produce a good which is the numeraire. Assuming free entry of firms and that output is the numeraire with a price of 1, that implies two zero profit conditions:

$$1) 1 = w_U \int_0^{\rho_C} \tau_U^C(x) dx + w_S \int_{\rho_C}^1 \tau_S^C(x) dx \quad (9)$$

$$2) 1 = w_U \int_0^{\rho_D} \tau_U^D(x) dx + w_S \int_{\rho_D}^1 \tau_S^D(x) dx \quad (10)$$

where, w_U is the unskilled wage, w_S is the skilled wage, ρ_C is the task dividing the U from the S tasks for technology C and ρ_D is the threshold task for the D technology.

Several key points follow from these two equations. First, together they imply a factor price invariance result as in standard trade theory. Because ρ_C and ρ_D are determined by the equality of the wage ratio to the marginal rate of technical substitution (MRTS) in profit maximizing firms and the MRTS is given by $\frac{\tau_S(\rho)}{\tau_U(\rho)}$ (i.e., is technologically determined), everything on the right hand side of both equations can be written as functions of w_U and w_S . That, combined with the assumption that these are general purpose technologies and so are producing the same good with the same price, implies that we have two equations in two unknowns (w_S and w_U). We show the solution diagrammatically in Diagramme D1. The figure shows the unit output isoquants for the two technologies. The isoquant for the centralized technology intersects the number of unskilled workers (N_u) axis at $n_{u0}^C = \int_0^1 \tau_U^C(x)dx$, i.e., the total number of hours to produce one unit if only unskilled workers are being used. Similarly, its N_s axis intercept is $n_{s0}^C = \int_0^1 \tau_S^C(x)dx$. The unit isoquant for the decentralized technology has a larger N_u intercept because of our assumption that unskilled workers take longer to do non-managerial tasks because of the requirement to communicate as well as produce but get no advantage in terms of the time they require to perform management tasks. In contrast, under the decentralized technology, skilled workers require no extra time to do non-production tasks and can take advantage of IT to spend less time on managerial tasks. The result is an isoquant with a larger N_u intercept, a smaller N_s intercept and a lower slope at all values of x than the C isoquant.²² Given the continuity assumptions and the comparative advantage assumption, the isoquants will cross once. That, in turn, implies that there will be a single unit cost line that is just tangent to the two isoquants, i.e., a single pair of w_S and w_U values at which both technologies are in operation.

²²To make the exposition simpler, we assume that $\lambda \cdot \gamma = 1$. This implies that the isoquant is smooth at task θ . Without it, there would be a kink in the isoquant that would complicate the exposition but not the ultimate conclusions.

Diagramme D1: Wage Setting with Two Technologies

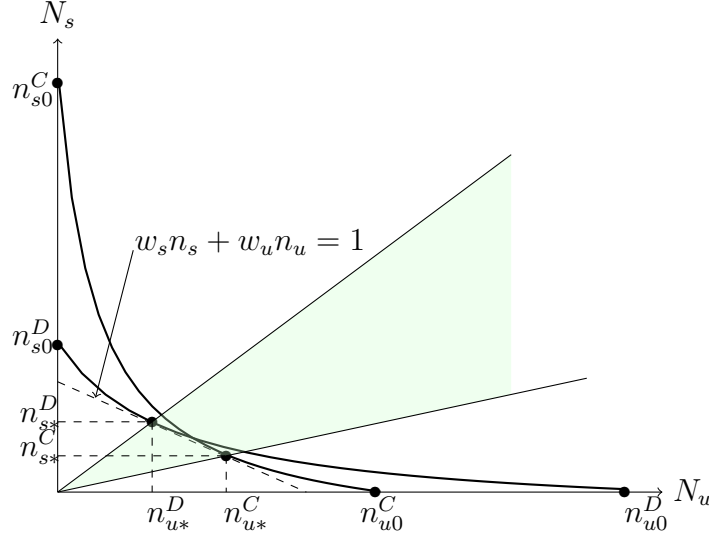


Diagramme D1 is, of course, a standard trade diagramme with two technologies instead of two sectors, and the same conclusions follow here as in the simple trade case. Our assumptions about the two technologies implies that the C technology will be relatively U intensive and in an equilibrium in which both technologies are used, n_{u*}^C and n_{s*}^C hours of unskilled and skilled work, respectively, will be used to produce a unit of the output with this technology. Similarly, n_{u*}^D and n_{s*}^D hours of unskilled and skilled work will be used with the D technology. Rays defined by $\frac{n_{s*}^C}{n_{u*}^C}$ and $\frac{n_{s*}^D}{n_{u*}^D}$ are drawn as diagonal lines in the figure. Those rays form the boundaries of the cone of diversification (the shaded area in Diagramme D1). As long as the ratio of skilled to unskilled hours in the economy falls within that cone, both technologies will be in use. If, instead, $\frac{N_s}{N_u} < \frac{n_{s*}^C}{n_{u*}^C}$ then only the C technology will be used. This is simple to see in the figure since on rays with lower slope than $\frac{n_{s*}^C}{n_{u*}^C}$, the cost line that is just tangent to the C isoquant will lie below the D isoquant, implying that it is less costly to produce just with C. Conversely, if $\frac{N_s}{N_u} > \frac{n_{s*}^D}{n_{u*}^D}$ then only the D technology will be used.

What is of most interest to us is the implications for wage movements when there are increases in S relative to U. Given that equations (9) and (10) have a unique wage solution and are not functions of labour quantities, as long as both technologies are in use, changes in the amounts of S and U in the economy do not alter the individual wages or their ratio. This is the standard factor price invariance result from trade theory. Firms in the economy react to larger relative amounts of S labour not by increasing the amount they use with any one technology but by shifting toward the more S intensive technology (D). In fact, it is straightforward to show that a given increase in the ratio $\frac{N_s}{N_u}$ generates

a more than proportionate increase in output from the D technology.²³

Following from this, the empirical implications from the model are as follows. First, if the two technologies are available and the skilled to unskilled labour ratio, $\frac{N_s}{N_u}$, is in the cone of diversification then increases in the ratio of skilled to unskilled labour does not alter the wage ratio, $\frac{w_s}{w_u}$, or the individual wages, w_s and w_u . Second, if $\frac{N_s}{N_u}$ rises enough then eventually all firms will adopt the D technology and then subsequent increases in $\frac{N_s}{N_u}$ will generate decreases in $\frac{w_s}{w_u}$ as in the standard one technology case. Third, assume that there are unskilled managers in the C technology before the increase in the skills in the economy (as is the case in our sample period), i.e., $\rho_C > \theta$. In that case, the ratio of the number of unskilled managers to skilled managers will decline as $\frac{N_s}{N_u}$ increases. This happens because U workers form a larger fraction of managers under the C technology (indeed, they may not be managers at all in the D technology given the comparative advantage set up) while S workers form a larger fraction of managers under the D technology. As the number of skilled workers rises, there will be a disproportionate shift toward the D technology that will imply more S than U managers overall even though the proportion of each type of manager will stay the same within each technology. Fourth, as $\frac{N_s}{N_u}$ increases, the proportion of S workers who are managers decreases. This is somewhat surprising given that the economy is shifting toward a more S intensive technology where more of the management positions are held by S workers. However, there is actually a smaller proportion of S workers who are managers with the D technology (since all S workers are managers in the C technology if $\rho_C > \theta$) and so as the economy shifts toward the D technology the proportion of S workers who are managers will fall. This is a reflection of the fact that in the decentralized technology, where S workers can both produce and communicate at the same time, S workers are used farther down into the task structure than in the C technology in equilibrium. Fifth, as $\frac{N_s}{N_u}$ increases and the economy shifts toward the D technology, we should see more workers in all parts of the production structure making decisions and communicating not just to their managers.

It is interesting to compare these implications to those from a more standard model with exogenous technical change. In Appendix B.8, we analyse a model in which one technology is in use at a time. The production function is expressed as a function of managerial and production labour with skilled workers having a comparative advantage

²³To see this note that we can write the ratio of S to U hours employed in the economy as a weighted average of the ratios employed in the two technologies, i.e., $\frac{N_s}{N_u} = \phi_C \frac{n_C^S}{n_{u*}^S} + (1 - \phi_C) \frac{n_D^S}{n_{u*}^S}$, where, ϕ_C is the fraction of output generated using the C technology. If the economy is in the cone of diversification, as $\frac{N_s}{N_u}$ increases, the two technology specific ratios do not change but ϕ_C decreases. In fact, ϕ_C must decrease more than proportionally to maintain the equality.

in managerial tasks. We characterize skill biased technical change as a relative increase in the productivity of skilled workers as managers. This captures both that the technological change favours skilled worker and that it related to managerial tasks. The technological change arrives exogenously, i.e., it alters the production function firms face without their making a choice over whether to adopt it. In this scenario, we show that the ratio of skilled to unskilled wages will remain constant only if the relative supply of skilled workers in managerial tasks increases by enough to offset the increase in their productivity in those tasks. This is the opposite of the implication from our endogenous technological choice model in which the expansion in S is accompanied by a decreasing proportion of S workers who are managers.

5 Evidence on Model Implications

5.1 Macro Evidence

We begin our investigation of the relevance of our model of choice between a decentralized and a centralized organizational form by examining the model implications in relation to the wage and employment patterns documented in the earlier sections of the paper. The first implication of the model is that the substantial increase in the proportion of workers with a university degree should have no impact on either the college premium or skilled and unskilled wages individually. In section 2, we showed that the college premium has not changed since 1992 even as educational attainment has soared and that this pattern cannot be explained as a result of compositional shifts in terms of observed or unobserved worker characteristics. This implication is borne out in our aggregate production function estimation where the coefficient on the relative skill supply variable in the wage ratio equations is small and never statistically significantly different from zero. As described earlier, the endogenous innovation model can also predict this zero effect but Acemoglu's description of the timing of the reaction of an economy to an increase in its relative skill supply involves an initial decline in the wage ratio followed by an increase as the effects of new inventions gradually take hold. In the figures in section 2, instead, the relative wage stays constant throughout the period of greatest education expansion - a pattern that is predicted by the technical choice model.

The technical choice model also has the stronger implication that underlying the lack of movement in the wage ratio should be a lack of response of the skilled and unskilled wages individually to the relative supply shift. As we discussed earlier, the

estimated coefficients on $\frac{S_t}{U_t}$ in Table 1 imply that movements in the skill ratio have no effect on either skilled or unskilled wages. These zero effects fit with the picture of the isoquant in Diagramme D1. In that figure the isoquant for the economy is formed as the envelope constructed using the Centralized isoquant to the right of n_{u*}^C , the straight line connecting the points, n_{u*}^C, n_{s*}^C and n_{u*}^D, n_{s*}^D , and the Decentralized isoquant to the left of n_{u*}^D . The flat portion of the isoquant matches a flat section of the aggregate production function corresponding to the range of factor employment values in which the economy is operating in the cone of diversification with both technologies in use. That section being flat corresponds to the effect of $\frac{S_t}{U_t}$ on the levels of both wages being zero, which we have just seen is true. It also implies that the determinant of the Hessian of the production function should equal zero. We can construct an estimate of that determinant as either, $(b_2 \cdot d_4 - b_4 \cdot d_2)$ or $(b_2 \cdot -d_3 - (1 - b_3) \cdot d_2)$. These take values of .007 and -.033 from the OLS estimates and -.16 and -.12 from the IV estimates, all of which are not statistically significantly different from zero at the 5% significance level and all but one of which are about the same size in absolute value as their associated standard errors. Thus, our production function based estimates fit with the model implication that the UK economy was operating in a region in which the production function had a flat spot in our time period. This is a very specific implication of our technological choice model. It is worth noting that one could allow ongoing technological changes in both the technologies in our model, which would be represented by inward shifts in the unit isoquants in Diagramme 1. However, if the rates of technological change were different in the two technologies then the wages and their ratios would change over time and the estimated production function would not have a flat segment. An equal technological change in each would be captured in a TFP measure that did not affect the wage ratio, as is the case in our estimates.

Taken together, we see the evidence from the production function estimates as fitting with technological change affecting the labour market through two channels. The first is a general shift out in the production possibilities frontier that is captured in our TFP measure. The fact that TFP changes induce wage level changes but no change in the wage differential implies that this element of technological change is skill neutral. It may reflect forces affecting productivity other than the IT and skill related changes that we emphasize here. Controlling for movements in TFP, changes in the skill ratio have no impact on wage levels or the wage differential, fitting with our model of endogenous technological choice. Thus, our evidence suggests a non-biased general shift out in the frontier with skill related technological changes corresponding to changes in the choice

of the point along a given frontier (i.e., holding TFP constant). The result that the economy is operating on a flat portion of the production function in this period is a key piece of evidence in favour of this view.

The other implications of the model at the aggregate level have to do with occupational composition. In particular, as the relative number of workers with BA's increases, management roles should be increasingly taken over by BA educated workers. Thus, the model predicts that the proportion of managers who have a BA should increase across cohorts. In the left graph of Figure 5, we plot the proportion of managers who have a BA over time. The plots are for 30 to 34 year olds in order to hold age composition constant. There is clear evidence of a large shift in the direction predicted by the model: approximately 25% of managers had a BA in the early 90s compared to over 50% after 2010.²⁴ At the same time, the proportion of the BA educated workforce employed as managers should decline according to the model. In the 2nd graph of Figure 5, we plot the proportion of BA workers employed in management jobs, again focusing on age 30-34. We see that 23% of BA workers were managers in the early 90s compared to 19% after 2010. We argued earlier that the pattern depicted in the two panels in Figure 5 fits with our model but does not match the predictions of a standard model with an exogenous technological change favouring educated workers.

5.2 Micro Evidence

We turn, next, to using micro data to examine the main implication of the model: that firms in locations with larger increases in the relative number of educated workers make greater use of decentralized organizational forms. Our hypothesis is that in a more decentralized and de-layered organizational structure, workers will be given more autonomy and will report greater influence over their work. We are interested in whether an increase in the relative supply of education skills induces a shift toward a more decentralized organizational form as measured by this marker. We examine this question using the UK Workplace Employment Relations Survey (WERS). The WERS is a survey of workplaces that includes questionnaires both for the manager as well as for a subsample of employees.²⁵ We focus on employees' responses to three questions:

²⁴The data underlying Figure 5 is from the LFS with managers corresponding to the first major group in the UK SOC2000, called 'Managers and senior officials'.

²⁵The WERS surveys 25 employees per workplace. When there are fewer than 25 employees at the workplace, they are all given the questionnaire. The WERS is a representative survey and we incorporate its associated weight in all our calculations.



Figure 5: BA proportion within managers, and Proportion of BA's Who are Managers

Notes: We define managers as the first major group under UK SOC2000. The occupation classification in the LFS changed from SOC90 in 2000 to SOC2000 in 2001, and then to SOC2010 in 2011. We map the other two classifications to SOC2000 in a probabilistic way, using a matrix from the ONS for the latter period, and a self-constructed matrix based on dual-coded data in 2000-1. The left graph shows the break points in the time series for when the classification changed.

“How much influence do you have about the following?”

1. “The range of tasks you do in your job”,
2. “the pace at which you work”
3. “how you do your work”.

The responses for each question range from 1 “A lot” to 4 “None”. These questions are included in the cross-sectional WERS surveys for 1998, 2004, and 2011. Rather than use these questions separately we implement a principal components analysis to compute an index of the ability of workers to influence their own work. We define the index as 4 minus the first principal component, so that the index is higher where more employees report having more influence. The index accounts for approximately 80% of the total covariance among the three questions. Finally, we normalize the influence index to have mean 0 and standard deviation 1 in the 3-wave-pooled sample. We view the answers of “A lot” to these questions as reflecting a decentralized workplace where decision making on what to do and how fast to do it has been devolved to workers. In this, we follow [Bresnahan et al. \(2002\)](#) and [Bloom et al. \(2012\)](#) who implement surveys of managers to capture organizational practices. Their decentralization measure is based, in part,

on "individual decision authority" which reflects whether workers control their "pace of work" and "method of work".

Table 3 lists the overall mean and standard deviation of the influence index by WERS wave and education of employees. Across all firms, there has been a nearly 0.6 standard deviation increase in the mean influence index value between 1998 and 2011. Thus, there is a clear general trend toward decentralization of decision making. We examine differences between more and less educated workers in the lower panels of the table, presenting weighted averages with the proportion of workers at a firm in the particular education group as the weights. Doing that indicates that the increases in the index value were particularly large at lower educated firms. This makes sense since those are the firms that would most likely have used a centralized structure in the past and that, as a result, would have had the most leeway for adjustment.

Table 3: Summary statistics of the influence index

Wave	Number of TTWAs	Number of workplaces	Mean influence index	Standard deviation
Influence index for all employees				
1998	204	1758	-0.32	0.92
2004	230	1657	0.024	0.96
2011	238	1917	0.27	1.025
Influence index for employees with degrees or above				
1998	190	1368	-0.018	0.79
2004	209	1272	0.001	0.83
2011	223	1557	0.13	0.80
Influence index for employees without degrees				
1998	203	1732	-0.34	0.88
2004	229	1620	0.024	0.93
2011	235	1823	0.25	1.047

Notes: for each education group or for 'all employees', we first calculate 4 minus the first principle component of the three influence scores (ranged 1 – 4). We then normalize that variable to have mean 0 and standard deviation 1 in the 3 wave pooled sample for the education group or for 'all employees'. Workplaces are weighted by the establishment's employment weight times the proportion of employees of that workplace in that education group. If a workplace has no employees of the labelled education group responding to the influence questions in the employee survey, the workplace is not counted in the sub-table for that labelled education group. *Source:* Authors' analysis of the UK Workplace Employment Relations Survey.

To investigate the role of skill supply in choice of organizational form, we examine the relationship between the local supply of workers with BAs and the influence index at the workplace level. "Local area" here refers to Travel To Work Areas (TTWA), which

were developed to capture local labour markets using data on commuting flows in 1991.²⁶ There were around 300 such areas in the UK in the 1998 through 2011 period. We derive from the LFS the proportion of workers in the TTWA who have a BA or above for the two calendar years up to and including the WERS survey year.²⁷

Table 4 reports the results from OLS regressions of the influence index on the local BA proportion across a range of specifications. In all the specifications, we pool together the data from the three waves and we weight by the size of the workplace. Given that our main variable of interest varies at the TTWA level, we cluster the standard errors at that level. In the first column, we report the results from an OLS regression with the proportion of BA's in the area and year dummy variables as the only regressors. The estimated year effects indicate a secular trend toward organizational forms with greater worker control. This may reflect a response to the general increase in the education level of the workforce but more direct evidence on whether such a relationship exists is found in the estimated effect of the proportion of workers with a BA. We estimate that a 10 percentage point increase in the proportion of BAs in an area is associated with a 0.09 standard deviation increase in the influence index. This result fits with the idea that firms in areas with a higher proportion of educated workers use more decentralized organizational forms.

In the next set of columns, we check the robustness of this result across a series of specifications. In the second column, we condition on the current HS proportion in the area, and the coefficient on the BA proportion changes very little. Thus, what matters for decentralization is the proportion of higher educated workers not more versus fewer high school drop-outs among the less educated. In the third column, we introduce controls for industry, workplace size, and size of the organization.²⁸ Notably, the size and significance of the BA proportion coefficient remains very similar to what was observed in column 1. This implies that the association between the level of education of the population and the organizational form happens within industries (as one would expect with a General Purpose Technology) rather than through shifts in the industrial structure. In the fourth column, we further include interactions between industry and wave and the key estimate

²⁶For further information on TTWA, see <http://www.ons.gov.uk/ons/guide-method/geography/beginner-s-guide/other/travel-to-work-areas/index.html>

²⁷For example, for the WERS outcome measured in 2011, the BA proportion is measured from LFS 2010-2011.

²⁸More specifically, industry is measured by the first digit of Standard Industrial Classification 1992; we have 5 categories of workplace size: <25,25-49,50-249,250-999,1000+. Whereas workplace size refers to the number of employees at the specific site, the organization may have multiple sites and hence many more employees. We have 5 categories of organization size: <50,50-249,250-999,1000-9999,10000+.

Table 4: Workplace-level regressions of the influence index

	(1)	(2)	(3)	(4)	(5)
Current %BA in the TTWA	0.92*** [0.17]	0.95* [0.50]	1.022*** [0.16]	1.01*** [0.16]	0.94*** [0.30]
Wave=2004	0.30*** [0.049]	0.30*** [0.045]	0.28*** [0.047]	0.44*** [0.14]	0.30*** [0.050]
Wave=2011	0.47*** [0.062]	0.47*** [0.066]	0.42*** [0.064]	0.77*** [0.22]	0.47*** [0.064]
Current %HS people in TTWA		0.047 [0.70]			
Dummies for workplace size, organization size and industry (1digit)	No	No	Yes	Yes	Yes
Full interactions between industry (1digit) and wave	No	No	No	Yes	No
Including London	Yes	Yes	Yes	Yes	No
Observations	5,332	5,332	5,332	5,332	4663
R-squared	0.064	0.064	0.155	0.165	0.156

Notes: All regressions are at the workplace level, with standard errors clustered at the TTWA level. Each workplace is weighted by its employment weight. For both the BA proportion and the HS proportion at TTWA, the variable is the proportion of economically active people (working or unemployed) in that education group from the LFS in the two calendar years prior to the year of the dependent variable. For example, for workplaces observed in 2004, the BA and HS proportions are from the LFS 2003-04.

Source: Authors' analysis of the UK Workplace Employment Relations Survey.

remains essentially unchanged. Finally, we are concerned that our results are being driven primarily by London as a potential outlier which contains a large number of observations and has both high education and high use of more modern technologies. However, omitting London, in column 5, does not alter our results.

In Table 5 we report results with the dependent variable generated either only from the responses of the BA employees or only from the non-BA employees' responses. The specification includes industry, size, and year effects as in column (3) of Table 2, and we try both weights based just on establishment size and weights based on employment in the specific education group. The results indicate that the positive correlation between BA proportion and employees' influence at workplace observed in the earlier specifications is not a mechanical result from a combination of BAs having more influence than non-BAs and an increasing proportion of BAs. In fact, the influence over work decisions reported by non-BA employees in their workplace is even more positively correlated with

the local supply of BAs than for BA employees. Again, this fits with the idea that under the older, centralized organizational form, BA employees would have had managerial or quasi-managerial roles and, thus, some control over decision making. It is the non-BA's who will experience the greatest change in the shift to a decentralized workplace.

Table 5: Influence by education of employees

	Influence Reported By			
	BA employees	non-BA employees	BA employees	non-BA employees
Weighted by	Establishment	employment	BA employment*	non-BA employment*
%BA in the TTWA	0.60*** [0.21]	0.86*** [0.24]	0.24 [0.20]	0.93*** [0.29]
Wave=2004	-0.011 [0.047]	0.28*** [0.040]	0.0088 [0.041]	0.29*** [0.0429]
Wave=2011	0.021 [0.052]	0.42*** [0.052]	0.092** [0.045]	0.43*** [0.059]
Observations	4,197	5,175	4,197	5,175
R-squared	0.08	0.121	0.062	0.143

Notes: The set of controls in each regression is the same as in column (3) in table 2.

* In the first two columns, each workplace is weighted by its employment weight. In the last two, the weight is multiplied by the proportion of employees in that education group. If a workplace does not have any employee in the education group responding to the influence questions in the employees' survey, it is omitted from the respective regression.

Source: Authors' analysis of the UK Workplace Employment Relations Survey.

Whether the estimated association between the local BA proportion and the average influence index value in these regressions represents a causal effect of the level of education is unclear. More educated workers may migrate to areas where firms have more decentralized organizational structures, implying a reverse causality. Alternatively, there could be a third unobserved factor prevalent in some areas that both increases the attractiveness of using a decentralized form and is attractive to more educated workers. We find it difficult to determine what form such a factor would take given that we are already controlling for industrial structure and firm size. In addition, the fact that our results hold up when we drop London (which is a strong candidate as a place where more educated workers migrate to with the aim of working for the most up-to-date firms) is weak evidence against the first endogeneity channel. Nonetheless, we are concerned that there is remaining endogeneity.

To address any remaining endogeneity, we adopt two approaches.²⁹ The first is to include the value of the dependent variable (the mean value of the influence index) in the first year for which we have it (1998).³⁰ One can interpret this variable as a parameterization of location fixed effects that uses only the part of the fixed effect that is correlated with the historic mean level of worker control over their workplace.³¹ Thus, we compare two regions with the same initial level of use of decentralized organizational forms as a means of holding constant a general proclivity to use such forms for time-invariant reasons and ask whether the region that had a greater increase in the proportion of workers with a BA saw a larger proportion of firms increase the extent of their decentralization. The results without industry and firm size controls are given in column (1) of Table 6 and the results including those controls are given in column (2). The estimated effect of the proportion BA is again highly statistically significant and takes a value of about two-thirds of the comparable estimates in the first and third columns of Table 3. Thus, the proportion BA variable is picking up longer term differences in the extent of use of decentralized forms to a limited degree and not enough to overturn our conclusion that increases in the proportion BA induces a movement toward those forms. Interestingly, the historical use of decentralized forms itself has only a weak relationship with future use of those forms in a region.

Our second approach is to implement an instrumental variables (IV) estimator. In particular, we make use of variation across areas that relates to the expansion of education. As instruments we use the proportion of the population born in the years 1970-74 and the proportion born between 1975 and 1979, measured in 1995-96.³² The underlying idea is that the proportion of the population with a university degree expanded substantially for the 1970s cohorts. As a result, areas with a high concentration of people of university age at the time of the expansion in the higher education system would be predicted to have a more educated population later to the extent that people have some tendency to stay where they grew up. In addition, we use the educational composition of people in the generation who would likely be the parents of these cohorts (people born between 1945 and 1954). In particular, we construct the proportion of the parental generations who have a BA and the proportion who have a GCSE/O level, again mea-

²⁹We implement these approaches using data aggregated to the TTWA. Estimation using data at the firm level with clustered standard errors yields very similar results.

³⁰Since we have to drop the first year of our data, we are left with firm observations across only two years of data.

³¹Direct fixed effect estimators yield erratic and ill-defined coefficient estimates which we interpret as arising from the shortness of our panel.

³²The denominator for the proportions is the population born between 1940 and 1979.

Table 6: Influence Index Regressions: Initial Value and IV Estimates

	(1)	(2)	(3) IV
Current %BA in the TTWA	0.62*** [0.20]	0.65* [0.23]	1.08*** [0.37]
Wave=2004	-0.21*** [0.049]	-0.17*** [0.048]	0.28*** [0.057]
Wave=2011			0.41*** [0.075]
Influence Index in 1998	0.025 [0.052]	0.051 [0.047]	
Dummies for workplace size, organization size and industry (1digit)	No	Yes	Yes
Including London	Yes	Yes	Yes
Observations	390	390	672
R-squared	0.119	0.278	
First Stage F-stat			15.35
Associated p-value			0.000

Notes: All regressions are at the TTWA level, weighted by employment, with standard errors clustered at the TTWA level. The instruments in columns (3) are: the population share of the 1970-74 birth cohort; the population share of the 1975-79 birth cohort; the proportion of BA educated individuals in the parents' generation; and the proportion of GCSE/O-level holders in the parents' generation. All the instruments are measured at the TTWA level in 1995-6.

Source: Authors' analysis of the UK Workplace Employment Relations Survey.

sured in 1995-96. We also include the interaction of these parental education variables with the size of the 1970s birth cohorts in the area. The idea behind the instruments is that areas that one would predict to have a large increase in the proportion of BAs in their workforce between the early 1990s and the early 2000s are ones where there is a local baby boom in those generations and where the parents own education indicates that they would be interested in their children's education. For this set of instruments to be valid, we require that parents in the previous generation - and, in particular, more educated parents - did not have a tendency to have more children in areas which would later turn out to have more decentralized organizational structures. We also require that the parents did not locate in an area because it would undergo a shift toward a more decentralized organizational form several decades later, as part of a shift to a technology that did not even exist at the time at which most of them made their location choice.

The fact that we control for industry and firm size effects in these regressions eliminates any concern that their location might have been related to persistent concentration in industries that would ultimately favour decentralization. We view the conditions under which this instrument set fails as very stringent. In particular, we find it hard to come up with situations in which differences in cohort sizes across areas are determined by the conditions that would affect the adoption of decentralized organizational forms decades later, especially after we control for industrial structure. The set of instruments are highly significant in the first stage, with p-values associated with the F-statistic for the test of their exclusion being effectively zero.

Column (3) in table 6 contains the results from our IV specification. The estimated coefficient on the proportion BA is 1.08, which is very similar to the value estimated with OLS in column (3) of table 3. This fits with our belief that endogeneity is not a substantial concern once we control for industry and firm size effects.

Our overall conclusion from our estimates is that an increase in the proportion of the working age population with advanced education in a region causes firms in that region to increase their use of decentralized technologies, with the effect being on the order of a 10 percentage point increase in the percentage of the working age population with a BA generating a 0.1 standard deviation increase in the extent to which workers feel they control their own work. This fits with results in [Caroli and Van Reenen \(2001\)](#) where they use UK and French data to show that a relative shortage of educated workers in a local labour market, as reflected in a higher education wage differential, implies that the firms in that market are less likely to implement organizational change. We view their results and ours as corroborating evidence for our model in which the large increase in the education level of new cohorts born after the late-1960s generated a shift in organizational structure toward a more decentralized structure in which workers had more control over their own tasks. As we have seen, in such a model, the technological shift can be accomplished without a change in the wage differential between more and less educated workers.

5.3 Other Technological Followers

To this point, we have presented evidence for a claim that the UK's combination of a rapid educational upgrading with no accompanying change in the education-wage differential can best be understood in the context of a model of technological choice in which the UK is a technological follower choosing among technologies developed elsewhere (most likely

the US). But the UK is not the only economy to undergo a substantial increase in its education level after the US, and it is worth asking whether other economies experiencing such an increase also have patterns fitting with them being technological followers.

To address this question, we use data from the OECD on the education levels and education-wage differentials for advanced economies between 1997 and 2010 (OECD (2012)). The data is from the labour force surveys for the member economies and is restricted to 25 to 64 year olds. The period is chosen both because it is one in which we can obtain consistent data and because it roughly matches the period of substantial growth in the UK's education level. That is, it is a period in which other economies also experiencing such growth would face the same set of existing technological choices. In this period, 11 other OECD economies both started the period with a proportion of their population with a tertiary education that was lower than that of the US in 1997 and experienced an increase in that proportion of at least 40%.³³ The lowest increase country meeting these requirements was Belgium (rising from 25% of its population having a tertiary education in 1997 to 35% in 2010) and the highest was Poland (moving from 10% with a tertiary education in 1997 to 23% in 2010). The OECD data indicates a 65% increase for the UK from 1997 to 2010, which is very close to what we obtain using the UK LFS for the same period (71%).

We examine movements in the wage ratio between the mean annual earnings of all workers aged 25 to 64 with a tertiary education and the mean annual earnings of workers with an upper secondary education being their highest education level. We regress this ratio on a simple linear time trend to summarize the wage differential pattern that coincides with the rapid educational growth in these economies. Out of the 11 OECD economies meeting our education growth criteria ³⁴: the time trend coefficient is not statistically significantly different from zero at the 10% level or below in 7; two exhibit statistically significant positive trends; and two exhibit statistically significant negative trends.³⁵ According to the time coefficient regressions, for Poland - the country with the largest percentage increase in tertiary education - the wage ratio fell by 1.8 percentage

³³The countries are: Australia, Belgium, France, Ireland, New Zealand, Norway, Poland, South Korea, Spain, Sweden, and Switzerland.

³⁴This includes the UK. We drop Australia because there are only 3 earnings observations in our period. For the other countries, the wage ratio data is for the years 2000 to 2010, with some missing years in most economies.

³⁵The countries with flat wage ratio profiles are: Belgium, France, Ireland, New Zealand, Poland, Switzerland and the UK. The two countries with positive trends are: South Korea and Spain. And the two with negative trends are: Norway and Sweden. Regressions of the wage ratio on the proportion with a tertiary education generate the same pattern of insignificant, significantly positive, and significantly negative coefficients on the education variable.

points per decade (from a base of 170). At the other end, for the country with the smallest educational increase - Belgium - there was a 1.5 percentage points increase per decade in the wage ratio (on a base of 130). The other economies with statistically insignificant time trends for the wage ratio show negative and positive point estimates that are either smaller or somewhat bigger than these two examples. We present the full set of estimated coefficients in Appendix B.10. In the appendix B.9 we also show how our estimates fit with previous results in Crivallero (2016), who estimates very small effects of increases in university attainment on the college wage premium in a pooled sample of 12 European economies, and Chen (2013), who shows that Taiwan also underwent a large increase in educational level with no accompanying change in its college premium.

Taken together, we believe the results in the OECD data and in other papers are consistent with our model for many economies undergoing substantial increases in their education levels. We make no claim that our discussion provides a complete analysis of the determinants of wage movements in these economies. The number of observations for each country in the OECD data is small and we do not investigate factors such as the level of decision making of workers, as we do for the UK. Nonetheless, we think the fact that there are so many economies which both start our period behind the US in their education levels and experience substantial educational growth but do not have statistically significant changes in their wage ratios indicates that it is plausible that other countries could also be described in terms of our model with educational catch-up driving endogenous technological choices. A more complete investigation of this hypothesis for other economies is beyond the scope of this paper.

6 Conclusion

In this paper, we highlight two empirical patterns: first, the UK underwent a dramatic increase in the proportion of the working age population with a BA since 1993; second, the BA-to-HS wage differential was essentially unchanged over this period. The combination of increased educational supply and a lack of movement in the educational wage differential necessarily implies a skill biased demand shift over time. We consider three models of technological change that imply skill biased demand shifts: the canonical model in which the demand shift is exogenous; a model in which the increase in education induces new skill favouring inventions; and a model in which a variety of technologies already exist, with firms choosing which to implement. We argue that the core patterns in the UK data do not fit with exogenous technological change models, including those

that incorporate tasks. Moreover, because the growth in educational attainment varies over time, the exogenous technological change models require that the rate of technological change has to speed up and slow down in just the right way to generate the pattern that we observe of an unchanging college premium throughout the post-1993 period. Of course, we cannot reject a claim that there just happened to be such a variation in the exogenous rate of technological change but we view it as improbable.

Of the remaining, endogenous technological change models, we believe that models of induced invention may be relevant for the US in recent decades since it was in a position to be a technological leader in skill biased technologies by virtue of having a much more educated work force than other developed economies at the dawn of the computer era ([Beaudry et al. \(2006\)](#)). In contrast, the UK underwent its educational expansion much later and, as a result, we believe it is plausible that it was a technological follower for this type of technology - following an induced technological adoption model rather than one of induced innovation.

More explicitly, we argue for a model for the UK in which firms in any sector can choose to produce using a centralized or a decentralized organizational structure as discussed in papers such as [Caroli and Van Reenen \(2001\)](#) and [Bloom et al. \(2012\)](#). In the decentralized structure, workers need to be able to take individual initiative and control their own work - characteristics that we view as fitting more with higher educated workers. The model has a similar construction to a classic trade model in that the economy responds to a shift in the relative supply of more educated workers by shifting toward greater use of the decentralized organizational structure. And, as in the trade model, there is no adjustment in terms of relative wages or wage levels. But the model also has further implications; most notably that the proportion of managers who have a BA should increase but the proportion of BA's who work as managers should decrease as the decentralized technology spreads. The latter is the opposite of the prediction from a standard skill biased demand model built around a nested CES production function. The model also implies strong restrictions on the shape of the aggregate production function that we show hold for the UK in this period. In addition, we show that areas in the UK which had more substantial increases in education levels are also areas where workers report having more control over their own work - something we see as a marker of a decentralized workplace. Importantly, this pattern occurs within industries, not because of shifts in the industrial structure, and is robust across a range of specifications. We develop an instrumental variable strategy in which we instrument for area specific educational changes using differences in fertility in previous decades and parental education.

We believe these instruments are very likely to be valid, based as they are on an assumption that parental decisions on fertility in the 1960s and 1970s did not arise from predictions of decentralized technologies coming to their areas in the 1990s and after. Again, it is important that we control for industry in all our specifications, implying that parents would have to make their guess about future technology use independently of the local industrial structure for our instrument to be invalid. The IV results indicate that increases in the education level in a local economy have a causal impact on the adoption of decentralized organizational forms by firms in that economy.

The key point we see as arising from this exercise is that the effects of technological change are not one size fits all. There are good reasons to believe the US has been a technological leader and there has been considerable study of the interactions of technological change and educational supply shifts in the US. The question then becomes, can the experience of the US be generalized to other countries? The UK provides an interesting case study to examine this question. Its large expansion in education happened quickly and well after the main expansion for the US. Because of that, we believe that the UK provides evidence on what happens to technological followers as their conditions shift toward favouring the technologies that the leader has developed. We argue that during the transition period for a follower economy, one could observe no real impact on skilled wage differentials even though the economy was being substantially transformed. Our evidence lines up with this interpretation. We believe this calls into question approaches in which technological change effects are identified from commonalities in wage and employment movements across countries, with remaining differences assigned to differences in institutions and differences in supply shifts. This does not mean that there are no commonalities across economies and that we should devolve to studying each economy in isolation. Instead, we view our results as indicating the need for a broader view of the impact of technological change - one which emphasizes the role of differences in movements in relative factor supplies in determining the point in the lifecycle of a technology at which each economy adopts it.

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A Appendix: Derivation of General Wage Equations

In this Appendix, we provide a more complete derivation of our aggregate skilled wage and wage ratio regressions given in equation (4) and (5) in the text.

Starting from the production function specification set out in the text and assuming competitive labour markets, we obtain,

$$\begin{aligned}\ln w_{ujt} &= \Omega_j - \frac{1}{\sigma_a}(\ln U_{jt} - \ln U_t) + \ln \theta_{ut} + \ln \frac{\partial F}{\partial(\theta_{ut}U_t)} \\ \ln w_{sjt} &= \Gamma_j - \frac{1}{\sigma_a}(\ln S_{jt} - \ln S_t) + \ln \theta_{st} + \ln \frac{\partial F}{\partial(\theta_{st}S_t)}\end{aligned}$$

Log linear approximations for these expressions are given in equations (1) and (2) in the text, and the approximation for the wage ratio is given in (3).

In order to take the skilled wage equation and the relative wage equation to the data we need to address the fact that the productivity parameter ratio ($\ln(\frac{\theta_{st}}{\theta_{ut}})$) and the θ_{ut} parameter that enter both equations are unobserved. We address these issues using the approach in [Beaudry and Green \(2005\)](#). In particular, we make use of the fact that given our production function we can write log TFP as,

$$\ln TFP_t = s_t^u \ln \theta_{ut} + s_t^s \ln \theta_{st} \quad (11)$$

where, s_t^u is the share of income going to unskilled labour and s_t^s is the share of income going to skilled labour. Rewriting (11) slightly, we have:

$$\ln \theta_{ut} = \frac{\ln TFP_t}{(s_t^u + s_t^s)} - \frac{s_t^s}{(s_t^u + s_t^s)} \ln \frac{\theta_{st}}{\theta_{ut}} \quad (12)$$

Note that if $\theta_{st} = \theta_{ut}$ then technological change is labour biased but not skill biased and bringing in TFP data alone would be sufficient to get estimable versions of (2) and (3).

To allow for skill biased technical change, we assume that the log ratio, $\ln(\frac{\theta_{st}}{\theta_{ut}})$ is a quadratic function of t , that is,

$$\ln \theta_{st} - \ln \theta_{ut} = \gamma_0 + \gamma_1 t + \gamma_2 t^2 \quad (13)$$

This allows for a bit more flexibility than the common linear skill biased technical change assumption, which is obviously nested in this specification.

Substituting (12) and (13) into the skilled wage equation yields an estimable speci-

cation similar to the one in [Beaudry and Green \(2005\)](#), given by:

$$\begin{aligned} \ln w_{sjt} = & \ln \Gamma_j + (\beta_1 - \beta_2 + 1 - (1 - \beta_2) \frac{s_t^s}{s_t^u + s_t^s}) [\gamma_0 + \gamma_1 t + \gamma_2 t^2] + (\beta_1 - \beta_2) \ln(\frac{S_t}{U_t}) \\ & + (1 - \beta_2) \frac{\ln TFP_t}{(s_t^u + s_t^s)} + \beta_2 \ln(\frac{K_t}{U_t}) - \frac{1}{\sigma_a} \ln \tilde{S}_{jt} + \epsilon_{1jt} \end{aligned} \quad (14)$$

Simplifying and gathering terms yields equation (4), the skilled wage specification, in the text. To ease comparisons with the existing literature, we estimate the coefficients on the t and t^2 terms as fixed, implicitly pinning the labour share values at average values for our period.

Similarly, we can write:

$$\begin{aligned} \ln w_{ujt} = & \ln \Omega_j + (\alpha_1 - (1 - \alpha_2) \frac{s_t^s}{s_t^u + s_t^s}) [\gamma_0 + \gamma_1 t + \gamma_2 t^2] + \alpha_1 \ln(\frac{S_t}{U_t}) \\ & + (1 - \alpha_2) \frac{\ln TFP_t}{(s_t^u + s_t^s)} + \alpha_2 \ln(\frac{K_t}{U_t}) - \frac{1}{\sigma_a} \ln \tilde{U}_{jt} + \epsilon_{2jt} \end{aligned} \quad (15)$$

and the difference between the two wage equations gives:

$$\begin{aligned} \ln \frac{w_{sjt}}{w_{ujt}} \approx & (\ln \Gamma_j + (1 + \beta_1 - \alpha_1 - \beta_2 - (\alpha_2 - \beta_2) \frac{s_t^s}{s_t^u + s_t^s}) [\gamma_0 + \gamma_1 t + \gamma_2 t^2] + (\beta_1 - \beta_2 - \alpha_1) \ln \frac{S_t}{U_t} \\ & + (\alpha_2 - \beta_2) \frac{\ln TFP_t}{(s_t^u + s_t^s)} + (\beta_2 - \alpha_2) \ln \frac{K_t}{U_t} - \ln \Omega_j) - \frac{1}{\sigma_a} (\ln \tilde{S}_{jt} - \ln \tilde{U}_{jt}) \end{aligned} \quad (16)$$

Simplification and gathering terms yields equation (5) in the text.

A.1 IVs for the skill supplies

In this section, we define the instrumental variables (IV's) for the skill supply variables in our aggregate production function estimation. The three IV's we use are:

$$IV1_{gt} = \sum_c \eta_{gc0} * BAgrowth_{ct} \quad (17)$$

$$IV2_{gt} = BAprp_{4550,g0} * BAgrowth_t \quad (18)$$

$$IV1_{gjt} = BAprp_{t-j-25,g0} * BAgrowth_{t-j,t} \quad (19)$$

where η_{gc0} is the share of cohort c in working-age population in region g at time 0 (1993-5), $BAgrowth_{ct}$ is the growth in the BA proportion among cohort c between time 0 and time t , in the UK as a whole, $BAprp_{4550,g0}$ is the BA proportion among the 1945-54

cohorts in region g at time 0, so as to capture the parents' generation of the 1975-84 cohort, $BAgrowth_t$ is the growth in the BA proportion between time 0 and time t , in the UK as a whole, $BAprop_{t-j-25,g0}$ is the BA proportion among the $t-j-25$ cohort in region g at time 0, so as to capture the parents generation of cohort $t-j$, and $BAgrowth_{t-j,t}$ is the growth in the BA proportion for the $t-j$ cohort between time 0 and time t .

The first two IVs are at the region-time level and are included as instruments for $\ln \frac{S_{gt}}{U_{gt}}$ while the third is at the region-age group -time level and serves as an instrument for $\ln \frac{\tilde{S}_{gjt}}{U_{gjt}}$. As seen in the first stage results, the first two IV's are highly significant in the first stage for $\ln \frac{S_{gt}}{U_{gt}}$ while the first and third instruments have substantial significant effects in the age specific skill supply and skill ratio first stages. The results imply easy passing of weak instrument tests.

Table 7: First stage results

	$\ln S_{gt}/U_{gt}$	$\ln \tilde{S}_{gjt}$	$\ln \tilde{S}_{gjt}/U_{gjt}$
IV_{gjt}	-0.354 (0.215)	3.146*** (0.647)	12.430*** (0.748)
$IV1_{gt}$	1.772*** (0.373)	-0.677 (1.124)	-0.446 (1.300)
$IV2_{gt}$	13.809*** (0.951)	-4.165 (2.863)	-20.169*** (3.310)
t	0.052*** (0.004)	-0.002 (0.011)	-0.004 (0.013)
t^2	-0.001*** (0.000)	0.000 (0.000)	0.000 (0.000)
$\ln \frac{TFP_t}{laborshare_t}$	0.016 (0.071)	-0.097 (0.213)	0.045 (0.247)
N	760	760	760

Notes: standard errors are shown in parentheses. The regression is at the level of 19 regions, 5-year-age-band and 3-year-period. The sample is restricted to 20-44 year olds. All specifications include complete sets of age-band dummies and region dummies. *** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

B Appendix (for online publication)

B.1 Alternative Production Function

A referee pointed out that a natural alternative production function given our main model could be written as:

$$Y = Y^C + Y^D \quad (20)$$

With,

$$Y^i = \theta_i F^i(U^i, S^i, K^i), i = C, D \quad (21)$$

where, Y is total output in the economy and Y^C and Y^D are output from firms using the centralized and decentralize technologies, respectively. Y is the sum of these two because they are alternative general purpose technologies (GPT's) producing the same output. Note that technological change, as captured in the θ 's is technology specific but factor neutral within each technology. As a result,

$$\ln TFP_t = s_t^C \ln \theta_{Ct} + s_t^D \ln \theta_{Dt} \quad (22)$$

i.e., it is a weighted average of the technology specific technological change factors, with the weights being the share of total income accounted for by the centralized, s_t^C , and decentralized, s_t^D , technologies. Given that we assume these are GPT's, there is no direct measure for these shares. However, in the theory, they will be directly related to the proportion of skilled and unskilled workers in the economy, so an empirically implementable version of 22 would use the skilled and unskilled labour income shares. That is, one arrives at a formulation that is the same as the one we implement. Given that we cannot identify one of these formulations from the other, we adopt the much more common specification in which technological change is skill enhancing.

B.2 The Role of Capital and Constrained System Estimates

In this appendix, we discuss the role of capital and TFP in wage specifications and present results when we impose theoretically implied cross-equation restrictions.

The regression equations (4) and (5) allow for general productivity growth but also incorporate a flexible skill biased technological trend. Many of the specifications estimated in the micro labour literature on technological change do not include either capital or TFP, and our specification obviously nests such an approach. In particular, if $\alpha_2 = \beta_2$

then neither TFP_t nor K_t appear in the relative wage equation. This would imply that capital is equally complementary with skilled and unskilled labour and would occur, for example, if the production function were multiplicatively separable in K_t and the overall labour component. That is what was assumed in the seminal [Katz and Murphy \(1992\)](#) paper and is one explanation for why most of the Skill Biased Technical Change (SBTC) literature and the polarization literature that followed use specifications that do not include capital. An alternative explanation not including capital comes from the combination of the constant returns to scale assumption and an assumption of a perfectly elastic supply of capital. It is straightforward to derive an expression for the price of capital and use it to substitute out the $\ln(\frac{K_t}{U_t})$ term in our two estimating equations. If we assume that the world price of capital is constant then here, as in the case with multiplicatively separable capital, we end up with the canonical specification for the relative wage equation with only a time trend and the relative skill supply variables on the right hand side.³⁶ We can, alternatively, allow the price of capital, r_t , to vary over time, implying an adjusted version of the canonical specification that includes $\ln r_t$ as a regressor. Estimates of this adjusted specification are available upon request. That specification yields very similar results in terms of the estimates of the coefficients of interest to those reported in the text.

The theory underlying our specifications implies several restrictions. Weak concavity of the production function implies that $\beta_1 - \beta_2 \leq 0$. From equation (14), the coefficient on $\ln(\frac{S_{gt}}{U_{gt}})$ in the skilled wage regression equals $\beta_1 - \beta_2$ and the estimates of that coefficient in both our OLS and IV estimates in Table 1 are negative. Second, concavity implies $\alpha_1 + \alpha_2 \geq 0$. We can construct an estimate of $\alpha_1 + \alpha_2$ as, $b_2 + b_4 - (d_2 + d_4)$, which takes on values that are slightly negative in the OLS and IV estimates (-0.11 and -0.15, respectively) but are not statistically significantly different from zero in either case. Thus, here too, we cannot reject the concavity restriction. The third concavity condition, corresponding to the determinant of the Hessian, is $(b_2 \cdot d_4 - b_4 \cdot d_2) \geq 0$. This terms takes a a value of -.16 with a standard error of 0.10. Thus, from the values estimated for all three conditions, we cannot reject the null of weak concavity of the production function.

The framework implies three equality restrictions on the regression equations (4) and

³⁶The two different approaches for eliminating capital from the relative wage equation have different implications for the skilled wage equation. If the production function is multiplicatively separable in capital and a labour aggregate then both TFP_t and K_t enter the skilled wage equation. If, instead, the production function is not multiplicatively separable in capital and labour but capital is perfectly elastically supplied then TFP_t but not K_t is present in the skilled wage equation. As with the relative wage equation, we can include $\ln r_t$ as an added regressor in the perfectly elastic capital supply case with a time varying price of capital.

(5): $b_3 + b_4 = 1$ and $d_3 + d_4 = 0$ and $b_5 = d_5$. The first restriction is clearly rejected in the OLS case while the other two are not rejected in any specification. In the first four columns of Table 8, we present SURE and IV estimates in which we impose these restriction and show that they make very little difference to the coefficients of interest, which are the coefficients on the skill supplies and the year effect. Overall, our parameter estimates fit well (albeit not perfectly) with the requirements imposed by our assumption that we are estimating parameters associated with a well-behaved production function. The last 2 columns of Table 8 contain IV results in which we add a cubic in time, showing that this extra flexibility does not alter our results.

Table 8: Skilled Wage and Wage Ratio Regressions: UK, 1993-2016

	$\ln \frac{w_{sgjt}}{w_{ugjt}}$	$\ln w_{sgjt}$	$\ln \frac{w_{sgjt}}{w_{ugjt}}$	$\ln w_{sgjt}$	$\ln \frac{w_{sgjt}}{w_{ugjt}}$	$\ln w_{sgjt}$
t	0.002 (0.006)	-0.006 (0.006)	-0.016 (0.009)	-0.001 (0.010)	-0.022* (0.011)	0.006 (0.010)
t^2	-0.000 (0.000)	0.000 (0.000)	-0.000 (0.000)	-0.000** (0.000)	-0.000 (0.000)	0.000 (0.000)
$\ln S_{gt}/U_{gt}$	0.056 (0.086)	-0.000 (0.081)	0.302* (0.144)	-0.156 (0.157)	0.307* (0.147)	-0.075 (0.136)
$\ln \frac{TFP_t}{\text{laborshare}_t}$	0.086* (0.044)	0.955*** (0.042)	-0.001 (0.076)	0.490*** (0.083)	0.099 (0.110)	0.373*** (0.102)
$\ln K_t/U_t$	-0.086* (0.044)	0.045 (0.042)	0.001 (0.076)	0.510*** (0.083)	0.104 (0.160)	0.145 (0.149)
$\ln \tilde{S}_{gjt}/\tilde{U}_{gjt}$	0.010 (0.012)		0.025 (0.029)		0.021 (0.037)	
time cubic					0.000 (0.000)	-0.000 (0.000)
$\ln \tilde{S}_{gjt}$		0.010 (0.012)		0.025 (0.029)		-0.057 (0.133)
IVs	no	no	yes	yes	yes	yes
constraints	yes	yes	yes	yes	no	no
N	1208	1208	760	760	760	760

Notes: standard errors are shown in parentheses. The regression is at the level of 19 regions, 5-year-age-band and 3-year-period. The sample without IVs consists of 20-59 year olds. Whenever we use IVs, the sample is restricted to 20-44 year olds. The first 4 columns are the same as the first 4 columns in Table 1 except that we now impose three constraints, and estimate using SURE and 3SLS rather than OLS and 2SLS. If we just use SURE and 3SLS and do not impose the constraints, the estimates would be very close to those in Table 1. The last 2 columns here are the 3SLS estimation of the two equations with IVs and a time cubic term; so they are the closest to the middle 2 columns in Table 1 - the only difference being the time cubic term. All specifications include complete sets of age-band dummies and region dummies. *** p<0.01, ** p<0.05, * p<0.1

B.3 Calibration Exercises Assessing the Applicability of SBTC Models for the UK

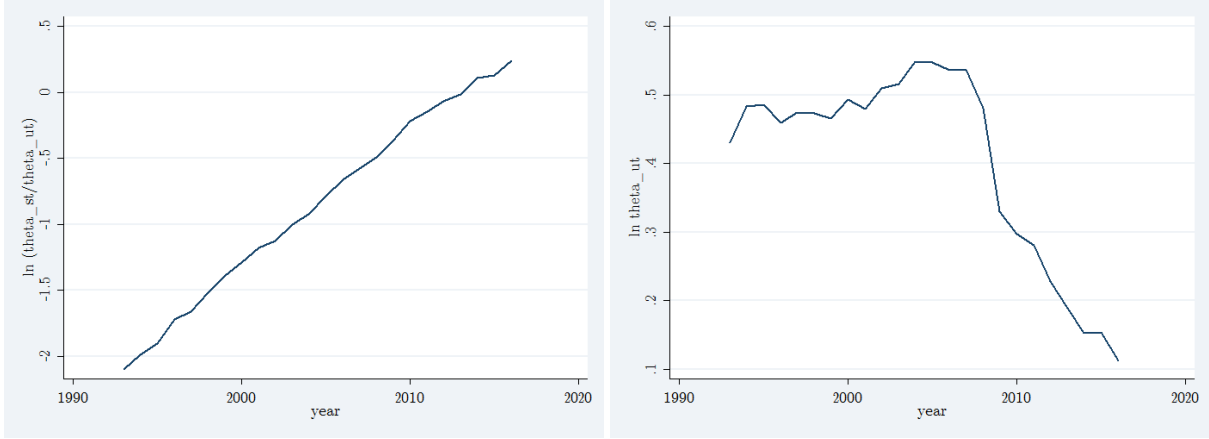
In this appendix, we calibrate the wage equations derived from our production function using typical elasticity values from the US literature and use that to back out skill specific productivity trends for the UK in order to see if the standard model delivers reasonable predictions about underlying movements in technology.

To carry out this exercise, we first assume that capital is equally complementary with skilled and unskilled labour so that the capital and TFP terms drop out of equation 3 and we arrive at a specification that is the same as that used in the previous US literature. Using elasticity values common to the literature (e.g., found in [Card and Lemieux \(2001\)](#)) of $\sigma=1.6$ and $\sigma_a=5$ and the observed trends in relative wages and relative labour supplies, we can back out an implied $\ln \theta_{st}/\theta_{ut}$ series.³⁷ We plot the resulting series in figure 6, showing that it increases by more than 2 log points over the 23 years of our data. Then, given this series and observed TFP we use equation 12 to back out an implied series for θ_{ut} . That series is weakly increasing until about 2008 and then falls by more than 0.4 log points between 2008 and 2016. We view the movements of both the $\ln \theta_{st}/\theta_{ut}$ and θ_{ut} series depicted in figure 6 to be too large to be credible.

We can enrich this exercise further by allowing capital to more complementary with skilled labour than unskilled labour ($\beta_2 > \alpha_2$). In our framework, $\beta_2 - \alpha_2$ is approximately the partial derivative of the log wage ratio $\ln w_s/w_u$ wrt $\ln K$, holding S, U constant. Krussell et al (2000) estimates that in the US capital equipment is more complementary with skilled labour, with $\hat{\sigma} = 0.4, \hat{\rho} = -0.5$. Their $\sigma - \rho$ roughly corresponds to our $\beta_2 - \alpha_2$. Therefore, we assume $\beta_2 - \alpha_2 = 0.9$ and back out a $\ln \theta_{st}/\theta_{ut}$ series from equation (16) in Appendix A. That series shows an increase of more than 5 log points over the 23 years. Again, this seems to us to be too large to be credible. Overall, the set of calibration exercises show that the basic patterns in the data, combined with standard estimated parameters from the SBTC literature yield implied skill specific productivity movements that are unrealistic. We see this as a different way of making the point that the SBTC model does not fit the UK data in our time period.

³⁷We average across age bands to remove age group effects.

Figure 6: Calibrated trend of $\ln \theta_{st}/\theta_{ut}$ and $\ln \theta_{ut}$



B.4 The expansion of high education in the UK and education classification

The expansion of higher education over the past few decades reflects a sequence of specific policy choices made by the UK government. Since the Robbins Report in 1963, policy related to the higher education sector has been moving toward implementation of the principle that university places ‘should be available to all who are qualified by ability and attainment to pursue them and who wish to do so’. The 1960s saw the foundation of more than 20 universities and dozens of polytechnics. Polytechnics were a form of higher education institution that taught both degree-level courses and below-degree-level courses, with their degrees certified by a chartered body called the Council for National Academic Awards (CNAA). A CNAA degree from a polytechnic was technically equivalent to a university degree and we treat them as equivalent in our analysis. The Education Reform Act (ERA) of 1988 changed some block grants to tuition fees (paid by Local Education Authorities for each student). In response, polytechnics increased enrolment with lower funding per student. The other major education policy change in 1988 was the replacement of CSEs and O-Levels with GCSEs as the exams that students take at age 16.³⁸ That reform led to an increase in educational attainment at the secondary level and hence an increase in the proportion of the young with sufficient academic credentials for potential admission to universities. In 1992, polytechnics gained the right to issue degrees and become fully-fledged universities. The reclassification of

³⁸Certificate of Secondary Education (CSE) and General Certificate of Education Ordinary Level (O-levels) were subject-based qualifications that students in England at the end of secondary school around age 16. CSEs are less academic, and so we count O-Levels in our definition of HS group (equivalent to GCSEs grade C or above), but not CSEs. CSEs are considered equivalent to GCSE below grade C.

polytechnics as universities led to a jump in the number of university students in 1992; but the rapid increase in student numbers in higher education started in 1988 and continued until 1994.³⁹ In 1994, pressures on public expenditures and a desire to protect resources per student led the government to introduce the maximum student number control. This limited the number of full-time undergraduates at individual universities per year. As a result, the growth in student numbers slowed. This acceleration and then deceleration can be seen clearly in the BA proportion across birth cohorts in Figure 9 in Appendix A.

This paper has focused on the comparison between two education groups: BA and HS. Here we show our main result that the BA-HS wage differential has been flat is robust to alternative definitions of education groups. In the paper, we have defined BAs as those whose highest qualification is first degree or higher, and HS as those who obtained Grade C or higher in the General Certificate of Secondary Education exam (GCSE) or equivalent and who did not have any degree-level qualification. We chose these definitions so as to be broadly comparable to college graduates and High School graduates in the US.⁴⁰

The first alternative we investigate is to draw the bottom line of the HS group at A-levels rather than GCSEs. A-levels are subject-based exams taken typically at age 18 and are a pre-requisite for university admission. Under the UNESCO’s International Standard Classification of Education (ISCED 2011), both GCSEs and A-levels in the UK are classified as level 3 - “upper secondary education”, and so are High School Diploma in the US. The left subgraph in Figure 7 shows that drawing the line at A-levels instead of GCSEs makes very little difference to the trend in the BA-HS wage gap.

Second, we group people by the age they left full-time education, and look at the wage gap between those who left at age 21-22 and those who left at 17-18. In Figure 7, we show the estimated trend (net of age effects) alongside the one based on our main definition of education, which was shown in Figure 2). Again, both trends are remarkably flat over the sample period. In summary, our main conclusion that the college wage premium has been flat since the early 90s is robust to how it’s defined.

Finally, we want to address the concern that the strong increase in the BA proportion observed in the Labour Force Survey may have been over-estimated due to sampling and measurement issues. The LFS is not a compulsory survey and its response rate has been declining over time.⁴¹ If graduates have a differential response rate to less-

³⁹This has been clearly shown in Figure 2 in [Carpentier \(2006\)](#)

⁴⁰For example, among 25-29 year olds in 2012, the US proportion of “BA” and “HS” are 35% and 56%. In the UK, the proportions according to our definition are 36% and 53%.

⁴¹The response rate can be found in the ONS Labour Force Survey Performance and Quality Reports.

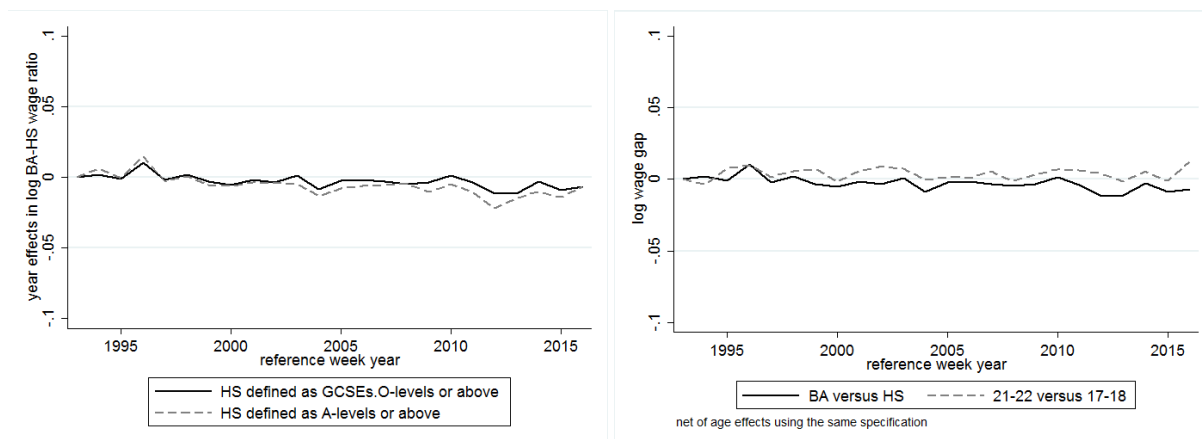


Figure 7: BA-HS log wage gap under alternative definitions

Notes: Same specification as Figure 2. The solid line in each graph is identical to the one in Figure 2.

educated people, the LFS may yield a biased estimate for the overall BA proportion. As a sensibility check, we obtain the number of graduates from the Higher Education Student Statistics (HESA)⁴². HESA collects student information directly from each university since the early 90s, so the graduate numbers are precise. We use the total number of UK-domicile students obtaining first degrees every academic year. This is plotted as the grey solid line in Figure 8.

Because information is collected at the time of leaving university, HESA statistics alone cannot tell us how many working-age graduates there are in total in the UK, or anything directly comparable with our Figure 1. So we use the LFS 2016 to derive its implied number of people obtaining first degrees every year. This is also tricky because the LFS doesn't tell us when people obtained each of their qualifications, only when they obtained their highest qualification. Thus, when we plot the number of people over the year they obtained their highest qualification (solid black line in Figure 8), the number overstates the truth in recent years. This is expected because for those with postgraduate qualifications, they must have obtained first degrees in some earlier unknown years. If we omit all the postgraduates as we do in the short-dashed line in Figure 8, then obviously we would under-estimate the truth. If we assume that all the postgraduates obtained their first degree at age 22 and add them to the last series, then we get the long-dashed line in Figure 8. This time series happens to be very similar to the HESA trend. In fact, all three measures from the LFS and the HESA one show a strong increase in

[Link](#)

⁴²The statistics start in 1994-5 and can be downloaded [here](#).

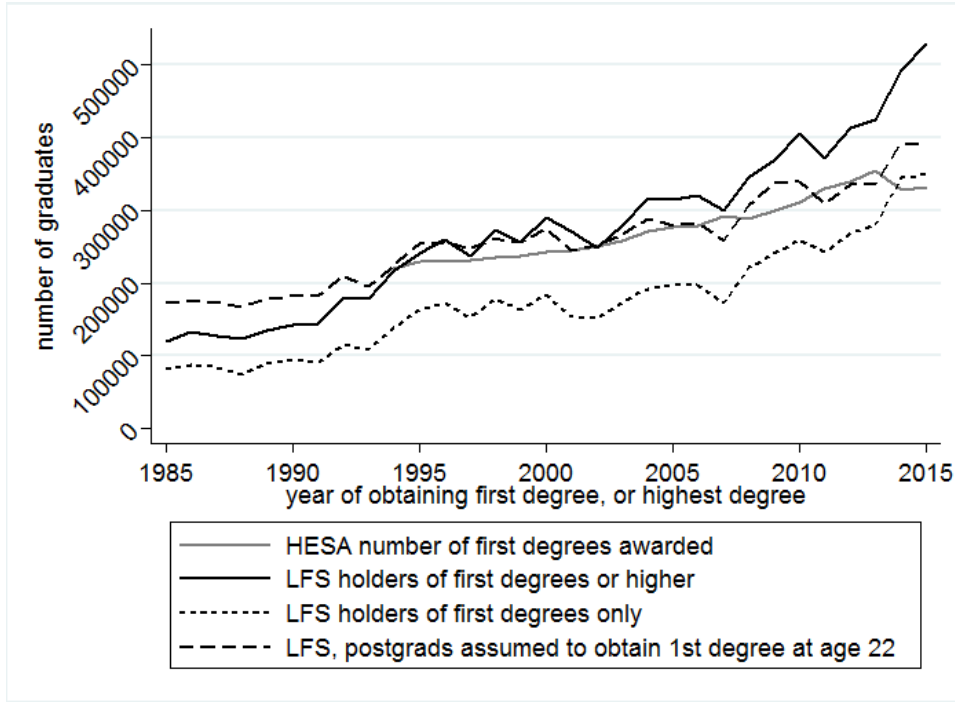


Figure 8: Number of first-degree graduates over year, HESA and LFS

Notes: the HESA series is the total number of UK-domiciled students obtaining first degrees by academic year, downloaded from [here](#). For all the LFS series, I add up the weight of UK nationals with at least first degrees by the year they obtained their first degree or highest qualification (up to 2015). As I use 4 quarterly LFS datasets in 2016, the weight is divided by 4 to gross up to population totals. The first LFS series counts all those with first degrees or above, by the year they obtained their highest qualification. The second counts those whose highest qualification is a first degree, by when they obtained it. The third assumes that all those with higher degrees obtained their first degree at age 22 and then counts everyone by the year they obtained their first degrees.

the number of new graduates over time. Together with the aging of less-educated older cohorts, this means the overall proportion of graduates in the working-age population increased rapidly since the early 90s.

B.5 Core Patterns by Birth Cohort

In section 2 in the paper, we aggregated the LFS data by 5-year age bands and year to examine time trends. Here we look at trends across birth cohorts. We aggregate the LFS data to the level of age and 5-year birth cohorts. The left subgraph of figure 9 shows the college wage premium over the life-cycle by cohort. The pattern is striking: the differential is increasing and concave over the life-cycle and there is not much difference across cohorts in either the shape or the level of the differential.

Unsurprisingly, when we regress these wage differentials on an age polynomial of order 5 and a complete set of cohort dummies, we find that the estimated cohort effects are quite flat. This is plotted in the right sub-graph of figure 9. The same graph also plots the cohort effects in the BA proportion, which is net of age effects in the way. It is clear that the BA proportion is increasing across cohorts and the increase was particularly sharp between the 1965-69 cohort and the 1975-79 cohort. This coincides with the timing of the HE expansion. As the UK Higher Education sector expanded rapidly from 1988 to 1994, the first cohort to be directly affected was born in 1970.

One may suspect that as the BA proportion increased so much, their quality, especially at the lower end of the BA quality distribution, may have fallen. If this is true, one may expect a fall in the wage gap at lower percentiles in the distribution. In Figure 10, we plot the cohort effects in the wage gap at various percentiles: the 10th, the 25th, the 50th, 75th and 90th. The trend across cohorts is relatively flat for all: the difference from the 1965-69 cohort is 0.1 log terms or less in absolute terms. The 10th percentile of the BA wage relative to the 10th percentile of the HS wage appears to have fallen a bit, by around 0.07 between the 1965-69 and 1975-79 cohorts. However, this decline in the wage gap was driven by a fast increase in the real HS wage at the 10th percentile, rather than a real wage decline among BAs at the 10th percentile. As shown in the 2nd sub- graph of Figure 10, the 10th percentile of the HS group grew by more than 15% between the 1965 and 1985 cohorts, when that of the BA group was about 10%, and growth was lower at the 25th and 50th percentiles for both groups. This decrease in within-group inequality, particularly for the HS group, looks like a natural consequence of the National Minimum Wage (NMW). The NMW was introduced in 1999 and has been raised at a faster pace than the median wage. Thus, there is no evidence of increasing supply of BAs reducing their relative wage in any part of the distribution.

B.6 Observable compositional changes

In this appendix, we present added investigations into compositional change effects. The first relates to the expansion of post-graduate degree holding.

The dark, solid line in Figure 11 plots the proportion of people with a postgraduate degree conditional on having a university degree. Similarly to what Lindley and Machin(2006) show for the US, the importance of postgraduate degrees increases for the UK in our period. Nonetheless, the proportion of postgraduates among university degree holders remains relatively low and so its change is unlikely to be a major driver of relative

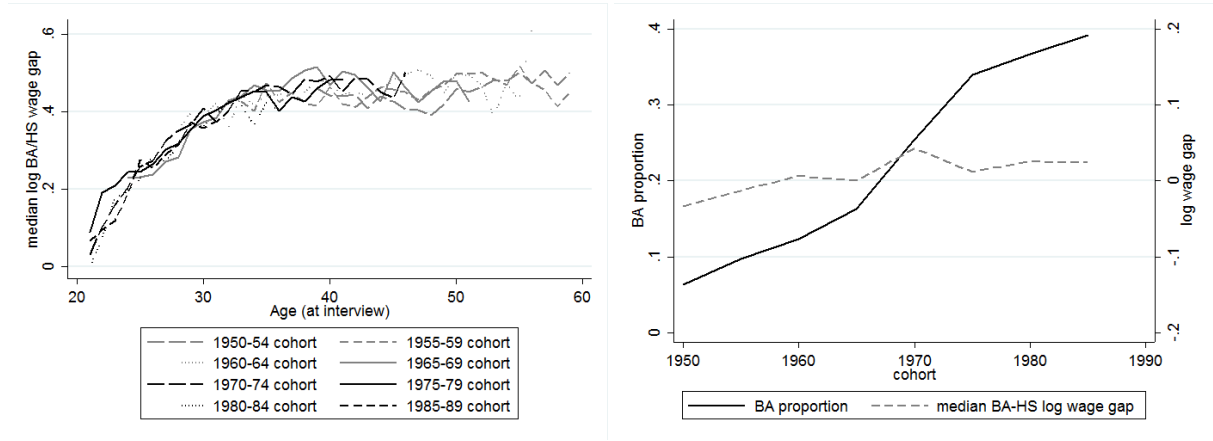


Figure 9: BA proportion and wage ratio over cohorts

Notes: We aggregate LFS data 1992-2016 up to the level of 5-year-birth-cohorts and age, where age is restricted to 20-59. We look at cohorts 1950-1985 only, so that each cohort appears many years in the data. The BA-HS median wage ratio is plotted at this level in the left sub-figure. For the right sub-figure, we regress the BA proportion on cohort dummies and an age polynomial of order 5. For the BA proportion, the cohort effects are scaled to the observed proportion for 1965 cohort at 30 year old. For the wage gap, the cohort effects are normalized to 0 for the 1965 cohort.

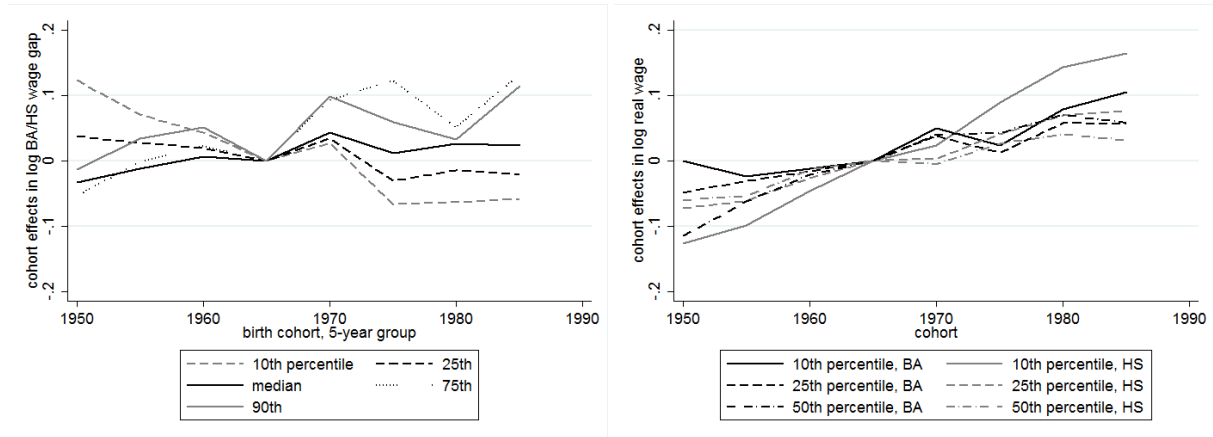


Figure 10: BA-HS wage ratio at different percentiles

Notes: We aggregate LFS data 1992-2016 up to the level of 5-year-birth-cohorts and age, where age is restricted to 20-59. We look at cohorts 1950-1985 only, so that each cohort appears many years in the data. For each percentile shown in the left graph, we regress the BA-HS log wage gap on cohort dummies and an age polynomial of order 5. The cohort effects are normalized to 0 for the 1965 cohort. For the right graph, the dependent variable is the real log wage for each of the shown percentile of the education group.

wage patterns. This is, in fact, what we see in the two wage gap lines in the figure. One line is a replotting of the line in figure 2, which includes postgraduate degree holders among the university graduates, while the other line shows the wage gap relative to high school educated workers when we include only those with exactly a bachelor's degree and no higher. The two lines are very similar, with both showing nearly identical values in 1993 and 2016.

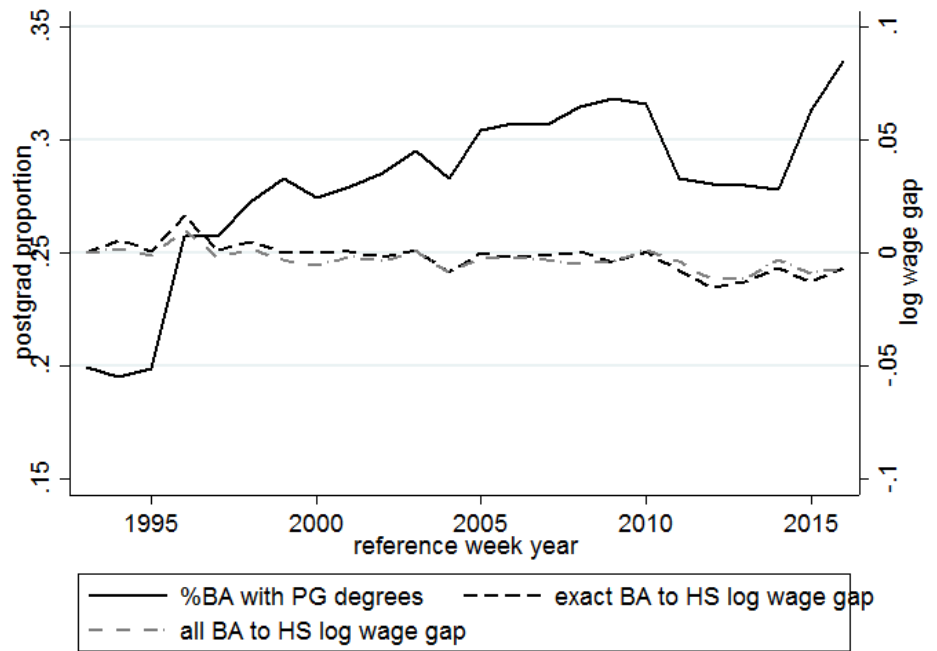


Figure 11: Year Effects for the Proportion of University Graduates with Advanced Degrees and the BA to HS Wage Ratio

Note: The year effects use the same sample selection and regression specification as for Figure 2.

The second compositional shift we consider relates to immigration. The proportion of UK workers without UK nationality has more than doubled over the past two decades, from under 5% to above 10%. As immigrants are more likely to have university degrees (as confirmed in Figure 12), the large flows of immigrants contribute directly to the aggregate increase in the share of BAs in the workforce. But it is not clear whether we should count every immigrant with a university education as the equivalent of a university educated native born worker. As demonstrated in [Dustmann et al. \(2013\)](#), immigrants often work in jobs that do not match their observed skills or qualifications, implying that a simple count of the number of immigrants with a university education may over-state

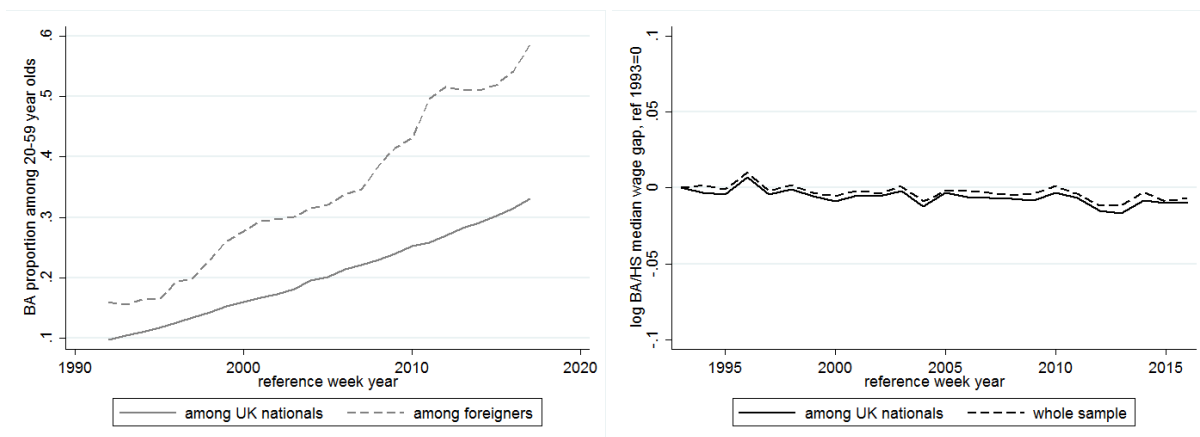


Figure 12: BA proportion and wage ratio over year, among those born in the UK

Notes: The BA proportions are not normalized. The year effects in wages are normalized to 0 in 1993. The whole sample series is the same as in Figure 2.

the contribution of immigration to the effective supply of highly educated labour. Given the size of the increase in the immigrant proportion in the past 20 years, the positive bias in the measured supply of university labour may become substantial. To address this concern, we can look at the BA-HS wage ratio among UK nationals only. Figure 12 shows that the BA-HS log wage gap is essentially flat and very similar to the trend including immigrants.

The second observable composition dimension we investigated was between public and private sectors. Public sector employees are, on average, better educated and, with wages largely protected from direct market forces, we might expect wage differentials within the public sector to be more rigid. Given that, an expansion in the public sector might partly explain the patterns we have described. That possibility, though, falls short in two ways with respect to employment numbers. First, the proportion of workers in the public sector does not change substantially over our data period. Second, the growth in the proportion of workers with a BA is very similar between the private and public sectors.

The public-private sector dimension of movements in wage differentials is a bit more nuanced. In Figure 13, we regress the wage differential at the year-age-band level on age dummies and year dummies and plot the year effects. The trend is slightly declining, but relatively flat. Compared to the whole economy (Figure 2), the private sector trend is slightly more decreasing: the change in the log wage gap over 22 years is about 0.03, rather than about 0.01 for the whole. This is still very small compared to what you might

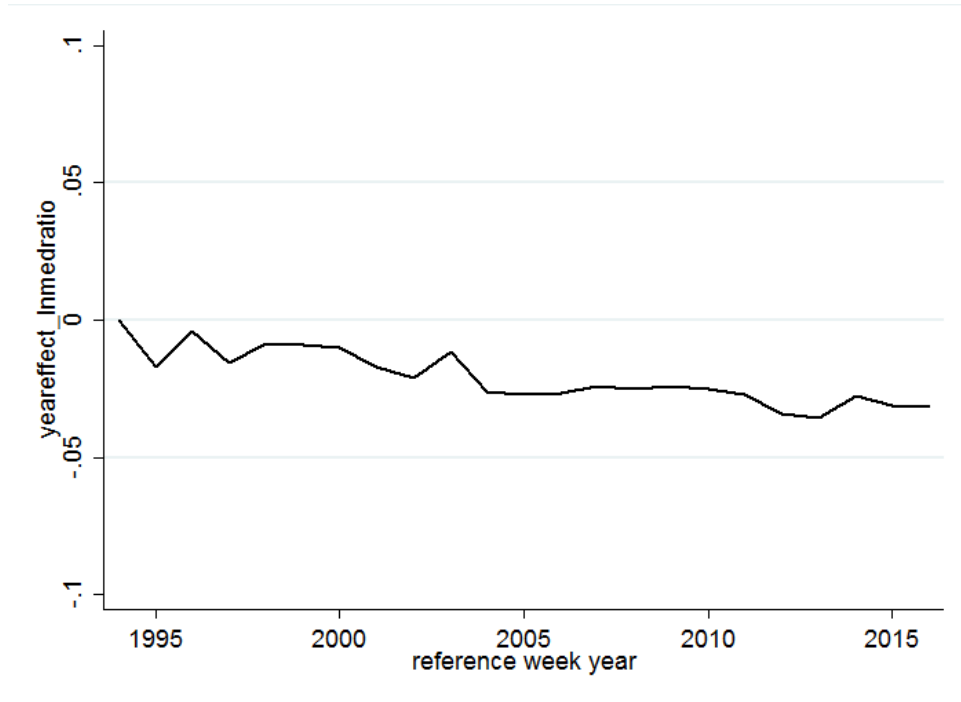


Figure 13: Time effect in BA-to-HS wage differentials, UK private-sector only

Notes: The time effect is normalized to 0 in 1994, because the variable on public versus private sector is available since 1994 only.

expect from an increase in the relative quantity of BA-to-HS (which is more than 1 full log point over the period).

One place we might look for a compositional shift is at the extensive margin: if the large increase in the relative supply of BAs combined with their constant relative wages induced a relative decline in the employment rate of BAs then this could imply changes in the relative “quality” of BA versus HS workers. In Figure 14, we plot the estimated year effects in the employment rate of BA’s and that of the HS population. The two series move very closely together over time. Thus, the lack of a relative wage response to the educational supply shift was not offset by a relative decline in employment. The change in relative employment rates is also small in the context of a near-tripling in the BA proportion over the period. Thus, we believe compositional shifts based on changes at the extensive margin are not a key driver of the main patterns.

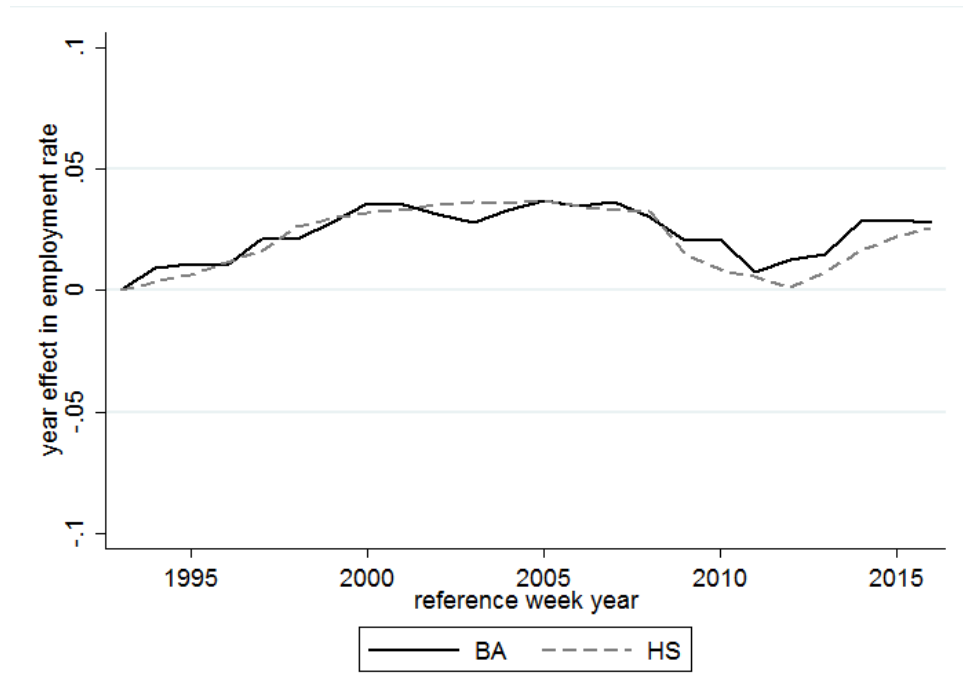


Figure 14: Time effects in employment rates among BAs and HS workers

Notes: The sample is LFS 1993-2016. The data is collapsed to the level of year and 5-year age bands and education. We then regress the employment rate on a complete set of year dummies and age-band dummies. The time effect is normalized to 0 in 1993.

B.7 Unobservable compositional changes: bounds

Implementation of a bounding approach rests on some (preferably minimal) assumptions about the model of wage determination. We will consider a simple but very standard model in which the wage for person i in education group j is given by:

$$\ln w_{ict} = \sum_{j=1}^3 D_{ijt} \beta_{cj} + \sum_{j=1}^3 D_{ij} f_{cj}(\text{age}_{it}) + \sum_{j=1}^3 D_{ij} \lambda_j \eta_i + \epsilon_{ict} \quad (23)$$

where c indexes the person's birth cohort, D_{ij} equals 1 if person i is in education group j , and zero otherwise, f_{cj} is a cohort-and-education-group-specific age profile of wages, normalized to 0 for age 30 and ϵ_{ict} is an idiosyncratic error that is independent across time and people and of all other right hand side components in the regression. The specification incorporates a person-specific ability factor, η_i , the effects of which differ across education groups according to loading factors, λ_j . Importantly, both the distribution of η_i and its factor loadings are stationary across cohorts. This model is extreme in its assumption of only one ability factor, but it is also very standard and allows us to see clearly the effects of selection.

We are interested in the price per efficiency unit of workers with a given type of education ($\beta_{cj} + f_{cj}(\text{age}_{it})$ in (23)). This is unobservable because we do not observe the median wage for a composition constant group. Below we will adopt some assumptions and bounds on the composition-constant median wage for each education group.

We shall assume that the values of the λ 's and other parameters are such that for each cohort, the three education groups correspond to three contiguous, non-overlapping ranges of ability. In particular, the groups are defined by two cohort-specific thresholds A_{uhc}, A_{hdc} . University graduates are those with $\eta > A_{uhc}$; high-school grads have $A_{hdc} < \eta \leq A_{uhc}$; and high-school dropouts have $\eta \leq A_{hdc}$. In theory, such a hierarchical model of selection could be rationalized by a Roy model where individuals choose education levels by comparing their expected net present value of wages and of costs, and assuming $\lambda_u > \lambda_h > \lambda_d$ and that the costs of obtaining education are weakly decreasing in ability. In addition, the hierarchical model fits the idea that university admission is largely rationed by prior attainment.

Consider a situation in which the university proportion increases between cohorts c and $c+1$, because there is less rationing. This corresponds to a decline in the value of A_{uhc} . Importantly, some individuals who would not get a university degree if they were born with their respective ability in cohort c will get a degree if they belong to cohort

$c+1$ but no one is induced to make the opposite switch. That is, there will be flows in only one direction. Let's call the set of individuals who would get a degree if they face the conditions in cohort $c+1$ but not if they were in cohort c , "joiners". Their ability distribution has a range with a top value of A_{uhc} and so it lies entirely below that of the rest of university graduates in cohort $c+1$. The latter group have abilities that are high enough for them to enter university even when the costs were higher (as they were for cohort c). We will call them "stayers".⁴³ Obviously, the joiners' ability distribution lies above that of those who remain in the HS group in cohort $c+1$.

The observed wage distribution of BAs in cohort $c+1$ is a combination of that of the joiners and that of the stayers. Under our assumptions, if the number of BA's increases across cohorts then that must reflect an inflow of joiners but no outflow. That means we can use the observed median wage for BA's in the first cohort as corresponding to the median wage of the stayers. In the second cohort, we can form two extreme bounds based on what we assume about the joiners. In the first, we could assume that all the joiners have lower ability than the median stayer. We could then form one extreme estimate of the median wage for stayers by first trimming a number of observations equal to the number of joiners from the bottom of the observed wage distribution for the second cohort and then getting the median of the remaining observations. For example, if the size of the BA group increases from 20 to 30 percentage points of the population between cohort c and cohort $c+1$ at a given age, then we trim the bottom one third of the BA wage distribution of cohort $c+1$ and the median of the remaining distribution is the upper bound of the median of the stayers. Another extreme bound could be formed by similarly trimming the top third of the cohort $c+1$ distribution and getting the median for the remaining sample. However, under an hierarchical model of the kind we are discussing, the best the joiners could be is as good as the stayers (if they were better than the stayers, they would be in the sector already). If they are as good as the stayers then the observed median wage for BA's in cohort $c+1$ would be the same as the median wage for the stayers. Thus, the observed median forms the other bound on the cohort $c+1$ median wage for the stayers. The next two pages explain mathematically why the trimming method and the observed median are THE upper and lower bounds under the hierarchical model. Differencing these bounds for the stayers' median wage in cohort $c+1$ from the observed median wage for cohort c then gives us bounds on the movements in

⁴³Calling them stayers and joiners is a slight abuse of terminology since we are considering different cohorts and so there are no individuals actually staying or joining. Instead, these groups correspond to different ranges in the stationary η distribution.

the price for BA labour for a composition constant group.

Because people (or, more properly, ability values) can be induced to switch into or out of higher education but not both at the same time, we can decompose the distribution function for BA wages in cohort $c+1$ into a component related to the distribution function for the “stayers” and a component for the “joiners”:

$$\begin{aligned} \Pr(\ln W_{uc+1} < w | \eta > A_{uhc+1}) &= p_{uc+1} \Pr(\ln W_{uc+1} < w | \eta > A_{uhc}) \\ &+ (1 - p_{uc+1}) \Pr(\ln W_{uc+1} < w | A_{uhc} \geq \eta > A_{uhc+1}), \forall w \end{aligned} \quad (24)$$

where, p_{uc+1} is the proportion of the university educated in cohort $c+1$ who are stayers. Equation (24) holds for any wage level w , but we are interested in a particular level: the median wage in cohort $c+1$ for the university sector stayers, denoted as $\tilde{w}_{uc+1}$.

We can write $\tilde{w}_{uc+1}$ as,

$$\tilde{w}_{uc+1} = \beta_{c+1u} + f_{c+1u}(\text{age}_{it+1}) + \lambda_u \text{med}(\eta_i + \epsilon_{ic+1t+1} | \eta_i > A_{uhc}) \quad (25)$$

Assuming stationarity of the η and ϵ distributions across cohorts, differencing this relative to the median conditional university wage in cohort c at the same age, age^* would yield,

$$\tilde{w}_{uc+1} - \text{med}(\ln W_{uct} | \eta_i > A_{uhc}) = \beta_{c+1u} + f_{c+1u}(\text{age}^*) - \beta_{cu} - f_{cu}(\text{age}^*) \quad (26)$$

That is, by comparing wage movements for people with the same set of η 's (the ones corresponding to choosing to get a university degree under either set of costs), we could obtain an estimate of the change in the actual wage profile across cohorts.

We cannot observe $\tilde{w}_{uc+1}$ because we are comparing across cohorts and so cannot see who has ability levels that would result in their choosing the university degree in the different rationing situations. But we can obtain bounds for it. Returning to equation (24), we can obtain an estimate of p_{uc+1} based on changes in the size of the u group between cohort c and $c+1$ combined with the argument that people (or, rather, ability levels) either enter or leave the group but not both. We know that the second term on the right hand side of (24) ($\Pr(\ln W_{uc+1} < \tilde{w}_{uc+1} | \eta > A_{uhc})$) equals 0.5 by the definition of $\tilde{w}_{uc+1}$, and the left hand side corresponds to a quantile of the conditional distribution of wages for the u group in the $c+1$ cohort, and so is calculable from the data. That only leaves the last term ($\Pr(\ln W_{uc+1} < \tilde{w}_{uc+1} | A_{uhc} \geq \eta > A_{uhc+1})$) unknown and unknowable. However, since it is a probability, we can bound it on one side as $\Pr(\ln W_{uc+1} < \tilde{w}_{uc+1} | A_{uhc} \geq \eta > A_{uhc+1}) = 1$, which corresponds to the marginal people

who obtain a degree in cohort $c+1$ but would not have done so in cohort c having wages that place them below the median wage for the group who would get a degree in either cohort. Based on this, we can get an upper bound on $\tilde{w}_{uc+1}$ by solving,

$$\Pr(\ln W_{uc+1} < \tilde{w}_{uc+1} | \eta > A_{uhc+1}) = \frac{1}{2}p_{uc+1} + (1 - p_{uc+1}), \quad (27)$$

This is equivalent to trimming the bottom $(1 - p_{uc+1})$ proportion of observations from the $c+1$ university wage distribution and obtaining the median of the remaining sample.

Since the abilities of university “joiners” between cohort c and $c+1$ are assumed to be entirely below the abilities of the “stayers”, a joiner’s wage can be higher than a stayer’s only when the joiner has a particularly positive shock ϵ_{it} or the stayer has a particularly negative shock. As the idiosyncratic shock is assumed to be independent of ability, it follows that the joiners’ wage distribution is first order stochastically dominated by that of the stayers. Mathematically,

$$\Pr(\ln W_{uc+1} < \tilde{w}_{uc+1} | A_{uhc} \geq \eta > A_{uhc+1}) \geq \Pr(\ln W_{uc+1} < \tilde{w}_{uc+1} | \eta > A_{uhc}) \quad (28)$$

Using the right side of this expression as the lower bound on $\Pr(\ln W_{uc+1} < \tilde{w}_{uc+1} | A_{uhc} \geq \eta > A_{uhc+1})$ in (24) implies that the right hand side of (24) just equals 0.5. That is, the other bound is the $c+1$ median itself.

Meanwhile, we can implement a similar exercise for the HS group. In this case, though, if the BA group grows between cohort c and $c+1$ this must be directly matched with an emigration of individuals from the top of the HS ability distribution between those cohorts. In trimming terms, this means that one bound can be obtained by appending a number of workers equivalent to the increase in size of the BA group to the top of the cohort $c+1$ wage distribution for HS workers. At the same time, if the Drop-out group shrinks then, under the single factor Roy model, they must have moved to the bottom of the ability distribution in HS and we would trim a number of workers equivalent to the decrease in size of the Drop-out sector from the bottom of the cohort $c+1$ HS distribution. Doing both the BA and Drop-out related trimming and appending yields a new adjusted HS sample in cohort $c+1$ that corresponds to one bound on the wages for the HS group stayers. Taking the difference between the median wage in that sample and the actual median wage for HS workers in cohort c yields an upper bound on the change in the log wage profile at a given age for HS workers. Consider the benchmark case where the upper bound scenarios for the BA and HS workers correspond to one another (i.e., the movements out of the top of the HS distribution become the movements into the

bottom of the BA distribution). We can then obtain one bound on the movement in the university - high school wage differential by taking the difference between the upper bound on the movement in the university median and the upper bound on the movement in the high school median. The other bound is the actual change in the median wage ratios shown in Figure 9.

We repeat the sample trimming exercise for each cohort using the 1965-69 cohort as the base of comparison (cohort *c* in our example). The resulting quality-adjusted wage differentials are reported in the left panel of Figure 15. The second panel shows cohort effects derived in the same manner as in the earlier figures. The cohort effects show an increase in the adjusted upper bound differential between the 1965-69 and 1970-74 cohorts. Given that the other bound is the actual change in the median wage ratio, the implication is that under this ability model, one cannot argue that selection on unobservables obscured what was actually a decline in the true wage differential. For the difference between the 1965-69 and 1975-79 differential, one bound shows a near zero change and the other shows a 4 percent decline. Thus, here there is some room to argue that selection is hiding a true decline in the ratio, but that decline is still very small compared to a doubling of the proportion of the population with a BA. For the post-1980 cohorts, the bounds include larger declines - about 15% relative to the 1965-69 cohort. However, a glance at the profiles in the left panel suggests the need for some caution in interpreting the cohort coefficients. The age profiles for the various cohorts no longer look parallel once the extreme bound trimming is implemented, implying that the age at which we evaluate the cohort differences can alter our conclusions. But, overall, our conclusion from this exercise is that, under this model of ability, selection on unobservables cannot explain why we do not see a large decline in the education wage differential for the cohorts with the largest increase in their education level.

B.8 Implications of Exogenous Skill Biased Technological Change with Managerial Tasks

In this appendix, we examine the implications of an exogenous skill biased technological change in the context of a standard production function that incorporates two skill levels and two broad types of tasks. The model exposition is similar in nature to that used in the Borghans and ter Weel (2008) paper on technology diffusion and the labour market. In particular, we consider a model in which one technology is in use at a time. Output, Y , is produced according to the Cobb-Douglas production function:

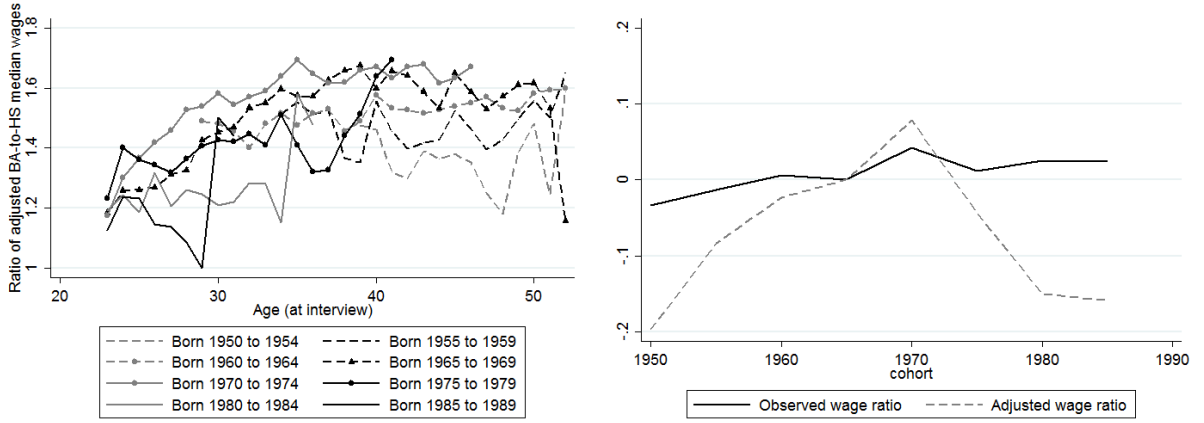


Figure 15: UK Median BA-to-HS wage ratio, adjusted to the education split of 1965 cohort

Notes: For each age and cohort, we adjust the wage distribution by using the proportions observed for 1965 cohort as reference points. For example, if the observed proportion of BAs is higher than that for the 1965 cohort at the same age, we would trim the bottom of the observed BA distribution.

$$Y = M^\alpha L^{1-\alpha} \quad (29)$$

where, M is hours of managerial labour, L is hours of production labour, and α is a parameter. Each task is performed by a combination of skilled and unskilled labour, with the labour aggregated through CES functions:

$$M = [aS_M^\sigma + (1-a)U_M^\sigma]^{1/\sigma} \quad (30)$$

and

$$L = [bS_L^\rho + (1-b)U_L^\rho]^{1/\rho} \quad (31)$$

where, $\frac{1}{1-\sigma}$ is the elasticity of substitution between skilled and unskilled labour in managerial tasks; $\frac{1}{1-\rho}$ is the elasticity in labouring tasks; a and b are parameters; S_M is the amount of skilled labour in the managerial task; and U_L is the amount of unskilled labour in the basic labouring task. We assume that skilled labour is relatively more productive in the managerial tasks (i.e., $a > b$) and that skilled and unskilled labour are more substitutable in the labouring task (i.e., that $\rho > \sigma$).

We assume that the numbers of unskilled and skilled workers in the economy are given exogenously in any period and that each worker supplies a fixed endowment of labour inelastically. Market clearing in the labour market corresponds to the total number of

workers with each skill level in the economy being equal to the sum of the numbers employed in the various occupations and technologies:

$$S = S_L + S_M$$

and,

$$U = U_L + U_M$$

Workers of each skill type can choose freely whether to work as a manager or a labourer and so there will be one skilled wage, w_s and one unskilled wage w_u .

In this framework, a skill-biased technological change can be represented as an increase in a , i.e., an increase in the productivity of S workers as managers. This captures both that the technological change favours S workers and that it is related to management tasks. Note that we are assuming that the technological change arrives exogenously and alters the production function of firms without them choosing whether or not to adopt the new technology.

To understand the impact of this change note that, working from the firm's first order conditions, it is straightforward to show that the wage skill ratio is,

$$\begin{aligned} \frac{w_s}{w_u} &= \frac{a}{1-a} \left(\frac{S_M}{U_M} \right)^{\sigma-1} \\ &= \frac{b}{1-b} \left(\frac{S_L}{U_L} \right)^{\rho-1} \end{aligned} \tag{32}$$

Rearranging these expressions slightly, we get:

$$\frac{a}{1-a} \frac{S_M^{\sigma-1}}{S_L^{\rho-1}} = \frac{w_s}{w_u} = \frac{b}{1-b} \frac{U_M^{\sigma-1}}{U_L^{\rho-1}} \tag{33}$$

In the context of this model, in order to match the main data pattern of an increase in S accompanied by no change in $\frac{w_s}{w_u}$, equation (32) shows that we need an increase in a of just the right size so that the skill biased demand increase just balances the relative supply shift. We view it as somewhat implausible that there were an exogenous set of technological changes that just balanced the supply shifts over an extended period of time, but we cannot reject that this could have occurred. Instead, we ask about the further implications of such changes if this were the mechanism driving our main data patterns. Examining (33), note that if a increases then the ratio of the number of skilled workers who are managers to the number who are labourers must also increase in order

to match the unchanging wage ratio. This is the opposite of the implication from our endogenous technological choice model in which the expansion in S is accompanied by a decreasing proportion of S workers who are managers.

B.9 Results on education expansion and wages in other countries

Our analysis fits with results in [Crivellaro \(2016\)](#). She uses two European surveys to examine wage and education patterns in 12 European countries between 1994 and 2009. Many of the economies in her data are in our sample of countries with substantial educational growth in this period.⁴⁴ and she shows that the proportion of the population who are tertiary education graduates for all of these countries pooled together goes up by 50% across the birth cohorts she studies. The dependent variable in the main exercise in the paper is the wage premium to having a tertiary or other post-secondary education relative to a high school diploma. This is regressed on a relative educational supply variable, a variable intended to capture skill biased demand shifts, and a complete set of country, year, and birth cohort effects. The results indicate statistically significant but very small relative supply effects with a 10% increase in the relative number of post-secondary to secondary graduates being associated with a 1.2% decline in the log wage ratio for the two groups in their OLS estimates. In addition, the relative demand effect is very small and not statistically significant from zero. Thus, Crivellaro's results with a set of 12 European economies matches closely with our results for the UK: substantial increases in education have little effect on the wage ratio and there is also little evidence of an ongoing skill biased demand shift.

Our results also fit with findings in some other papers examining wage differentials and education increases in other economies. [Chen \(2013\)](#) examines these patterns for Taiwan, which underwent a dramatic boom in creating new post-secondary institutions between 1990 and 2000. As a result of that boom, between 1990 and 2010, the number of post-secondary graduates increased by a 600%. Yet over that same period, the difference between the mean log hourly wage for university graduates and workers with less than a university education was quite flat. That university wage premium was approximately 0.6 in 1980, 1990, 2000, and 2010. Chen interprets this outcome within an exogenous skill biased technological change model. As we argued earlier, for such a model to generate

⁴⁴The countries in her data are: Austria, Belgium, Germany, Denmark, Spain, Finland, France, Greece, Ireland, Italy, Portugal, and the UK.

a flat premium trend requires a lucky, exact balance of relative supply and exogenous demand shifts. We believe that our model, in which the flat profile provides a more natural explanation. [Choi and Jeong \(2005\)](#) and [Choi \(2015\)](#) examined a similarly large increase in education levels driven by policy changes in South Korea in the 1980s and 1990s. Between 1990 and 2005, the proportion of high school graduates who enrolled in a post-secondary programme increased from approximately 30% to 80%. [Choi and Jeong \(2005\)](#) show that the post-secondary wage premium declined in the 1980s but was flat during the substantial educational expansion that started in the mid-1990s. They show that the latter patterns coincided with an increase in expenditures on IT and conclude that the flat premium reflected an endogenous technological change model. These trends could fit with our model, with the initial decline in the wage premium in the 1980s corresponding to a period before the economy entered the cone of diversification. The post-1994 period is then the period of transition to taking up more skill-biased technologies, as evidenced by the coinciding increase in IT expenditures. Finally, [Carneiro et al. \(2014\)](#) examine wage impacts of an earlier large increase in post-secondary attainment in Norway, taking advantage of regional variation in the creation of universities in the 1970s. They show that the regions where new universities were added had a significant jump in the education level of their workforce but that the wage differential between university and high school educated workers either stayed flat or increased. They interpret this within the context of an endogenous technological change model and show evidence that the productivity of skilled workers increased in relative terms in the regions with new universities.

B.10 OECD Data on Wage Differentials

In this appendix, we present the results from a simple exercise based on the data on educational attainment and wage differentials from [OECD \(2012\)](#). As mentioned in the text, we focus on the set of OECD economies that have a lower proportion of their population than the US with a tertiary education in the initial year of the data (1997) and experience a growth in that proportion by at least 40% by 2010. In the table, below, we present estimates for this set of countries from a regression on a constant and a linear trend of the wage ratio between the mean annual earnings of all workers aged 25 to 64 with a tertiary education and the mean annual earnings of workers with an upper secondary education being their highest education level. Of the 11 countries meeting our criterion, 7 have trend coefficients that are not statistically significantly different

from zero, 2 have positive and significant coefficients, and 2 have negative and significant coefficients.

Table 9: Regressions of Wage Differential on a Time Trend by Country

Country	Const	t
Belgium	30.02** (2.19)	0.15 (0.23)
France	47.25** (4.24)	0.036 (0.46)
Ireland	47.84** (12.2)	1.47 (1.2)
Korea	31.82** (7.26)	1.86* (0.73)
New Zealand	22.26** (2.9)	-0.28 (0.3)
Norway	31.98** (0.91)	-0.33** (0.11)
Poland	72.66** (6.58)	-0.18 (0.68)
Spain	19.63** (2.88)	1.72** (0.3)
Sweden	32.57** (1.06)	-0.58** (0.11)
Switzerland	57.76** (2.12)	-0.21 (0.21)
UK	58.59** (2.81)	0.045 (0.29)

Authors's calculations based on data from [OECD \(2012\)](#). Standard errors in parentheses.

*, ** statistically significant at the 1% and 5% significance levels, respectively.